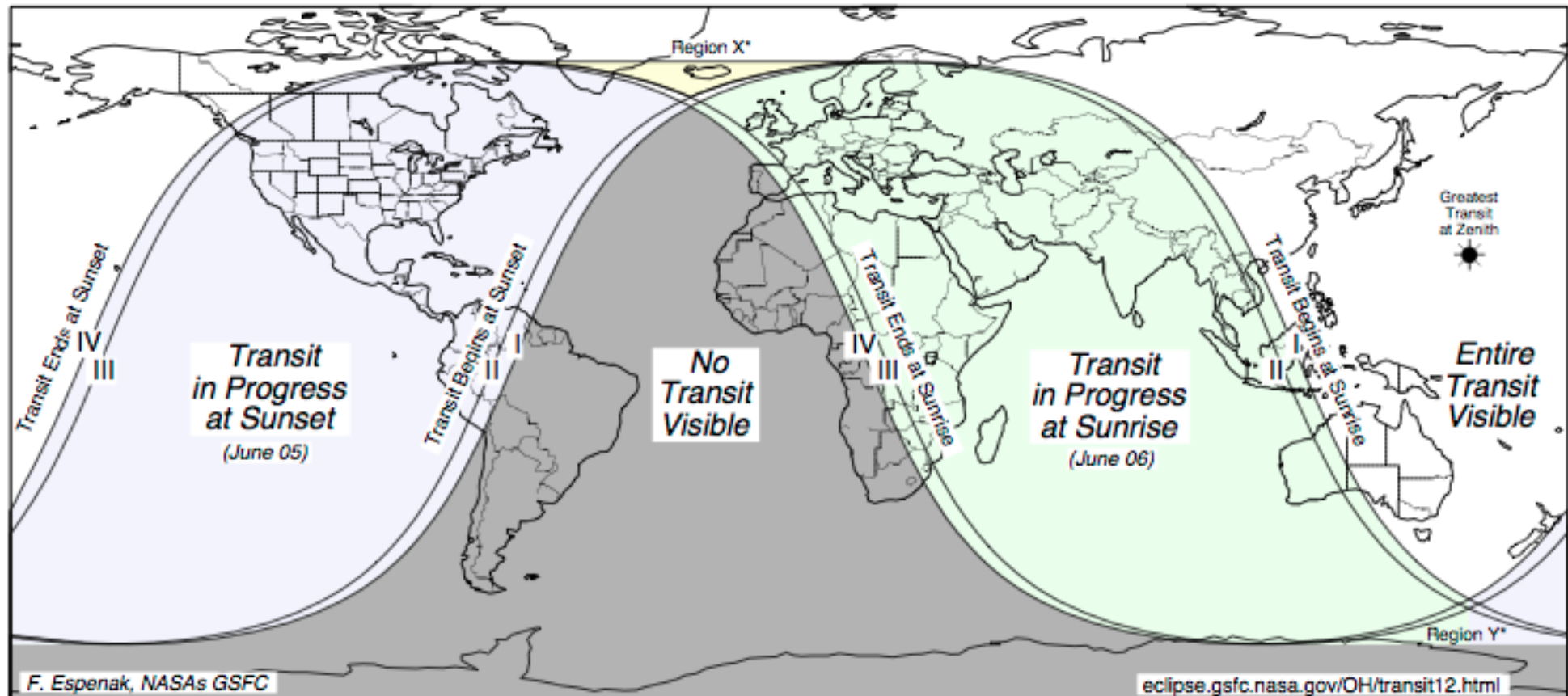


Venus in sole visa



Davor Krajnović

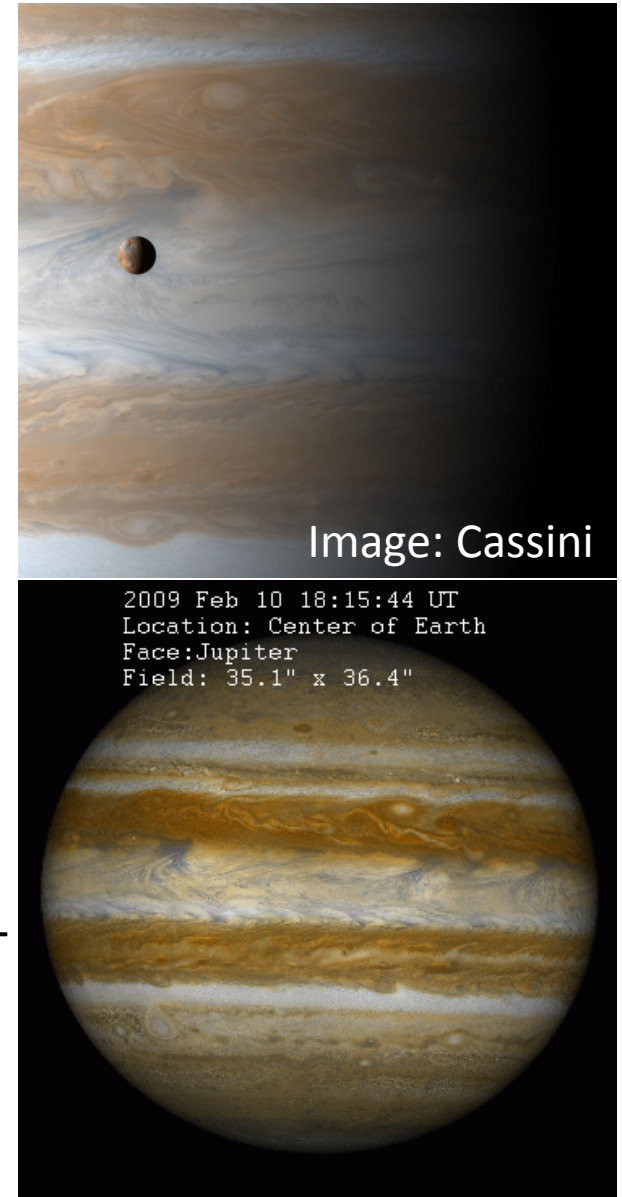
Global Visibility of the Transit of Venus of 2012 June 05/06



- Venus starts exiting the Sun disk (3rd contact): 06:37:40.7 am (CEST)
- All finished (4th contact): 06:55:10.1 (CEST)
- Sunrise: 05:15

What is a Transit?

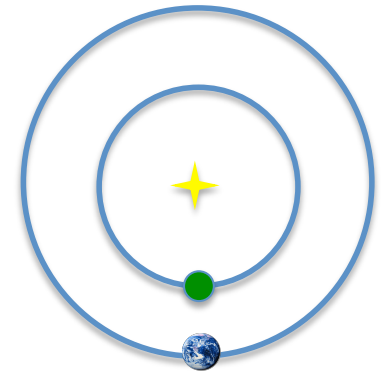
- Transit:
 - occurs when a body appears to move across the face of another body
 - The apparent size of the transiting body is SMALLER than the background object
- Occultation
 - Same as transit, but the body that transits occupies the most of the background body (or completely hides it)
 - The apparent size of the transiting body is LARGER than the background object
- Eclipse
 - When a body (partially) disappears during an occultation
 - Solar eclipse: Moon occults the Sun
 - Moon eclipse: Earth occults the Moon (Moon in the shadow of Earth)



Source: wikipedia

Why isn't Venus in transit every year?

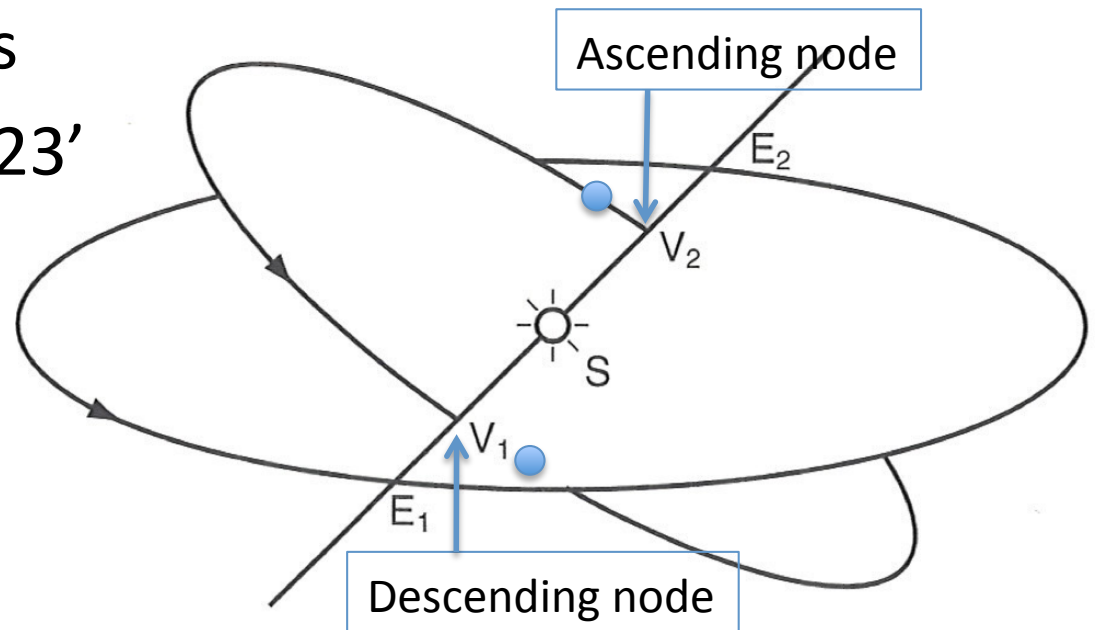
- Orbits of Earth and Venus!
 - Venus year: 224.7 days
 - Earth year: 365.256 days
 - 13 Venus years = 8 Earth years
- Synodic period = 583.9169 days
 - 5 x Synodic period = 2919.58 days
 - 8 x Earth year = 2922.05 days
 - Every 8 years Venus and Earth occupy nearly the same position in space (relative to fixed stars)
 - Difference: 2.46 days
 - ➔ every 8 years Venus is 22' further on its orbit



Inferior conjunction

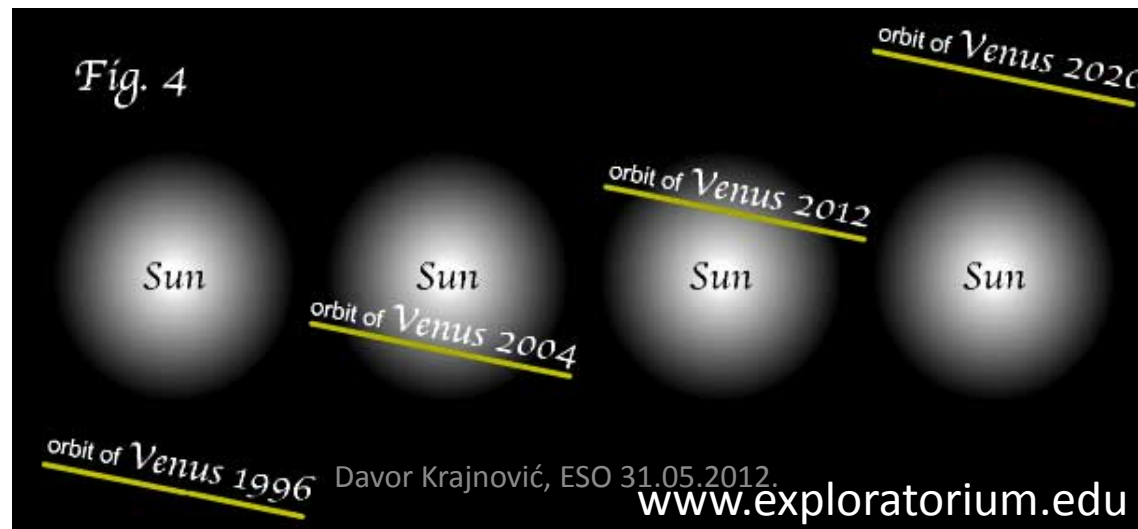
Why isn't Venus in transit every year?

- Transit occurs when Earth crosses the line of nodes at the same time as Venus
- Tilt of Venus orbit = $3^{\circ} 23'$ wrt ecliptic
- Venus is
 - around 8 Dec at its ascending node
 - around 7 Jun at its descending node
- Venus is faster than Earth
→ every 8 years Venus is $22'$ higher or lower in its orbit



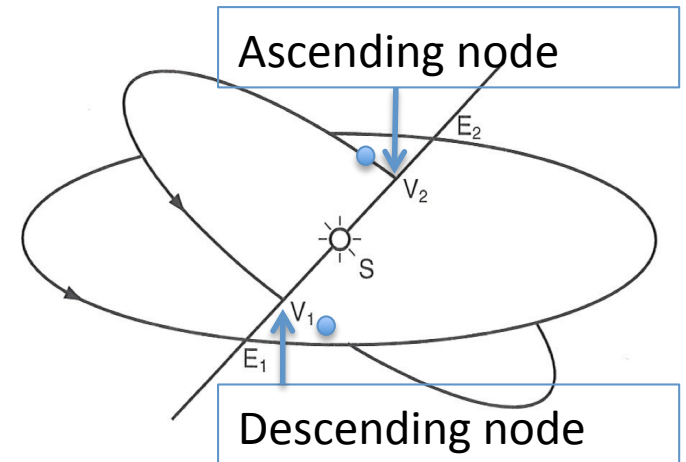
Will it happen?

- Assume that we see Venus in the middle of the Sun disc today
- Sun disc is 32' in diameters
- In 8 years Venus will be 22' above (or below) the point we see it today → it will miss the Sun!!
- If it is closer to Solar limb → it will cross it again!!
- Venus transit happen in pairs of 8 years (3x8 not possible!)



Complex, but periodic

- Earth's & Venus' paths are not circles, but ellipses
 - Speed changes as a function of position on the orbit
 - Distance to Sun (Sun's apparent size) changes
 - Gravitational influence of other planets...
- The present schedule:



A	A			D	D			A	A			D	D			A
8	121.5			8	105.5			8	121.5			8	105.5			

←
→

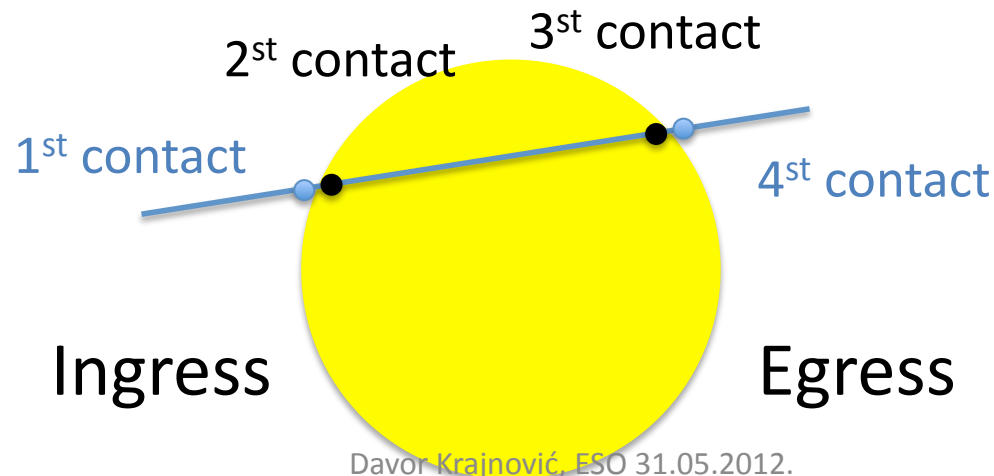
←
→

243
243

Some other features

- Venus goes from East to West across the Sun
- June and December transits are not fixed to a date
 - Retrograde motion of Venus' line of nodes
 - Retrograde motion of Earth rotation axis (precession of the equinoxes)
 - ➔ 29.8" per year
 - during 243 period ➔ delay of ~2 days

7.12.1631	6.6.1761	9.12.1874	8.6.2004	11.12.2117	11.6.2247
4.12.1639	3.6.1769	6.12.1882	6.6.2012	8.12.2125	9.6.2255



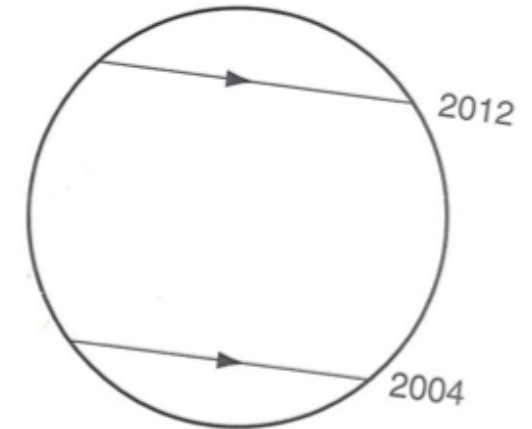
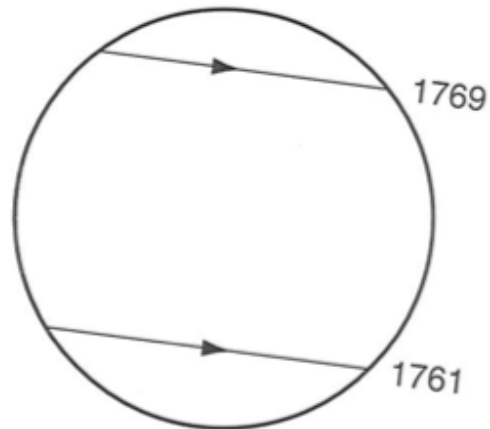
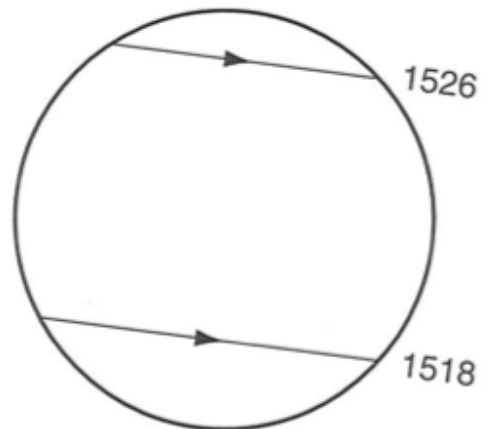
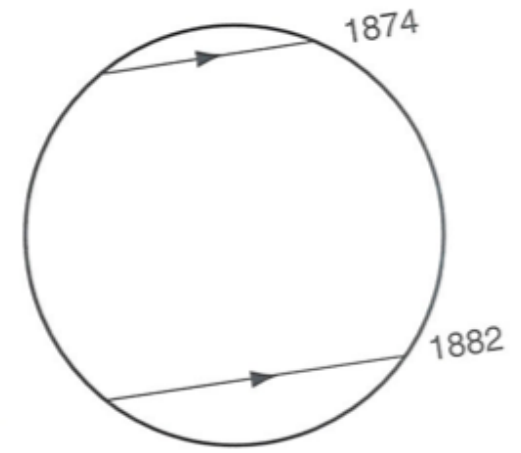
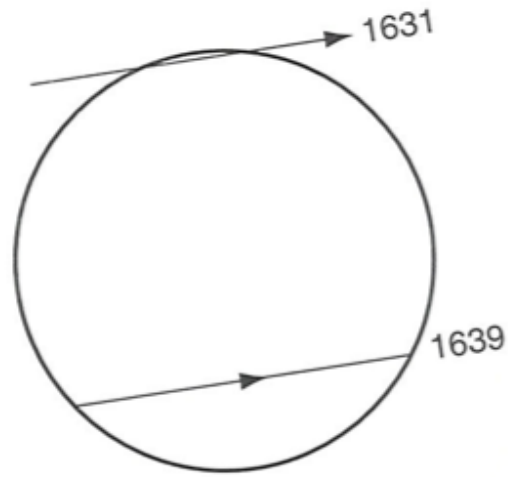
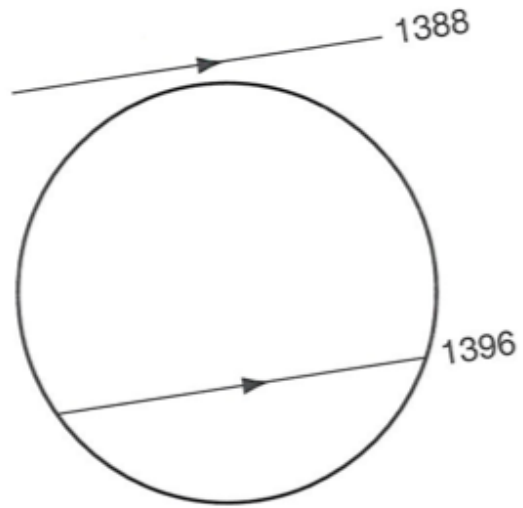
Transit of June 8, 2004



Davor Krajnović, ESO 31.05.2012.

Portugal, movie by ESAC

Past transits

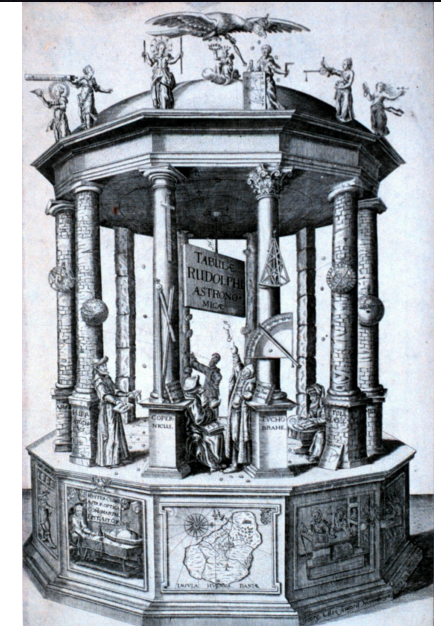
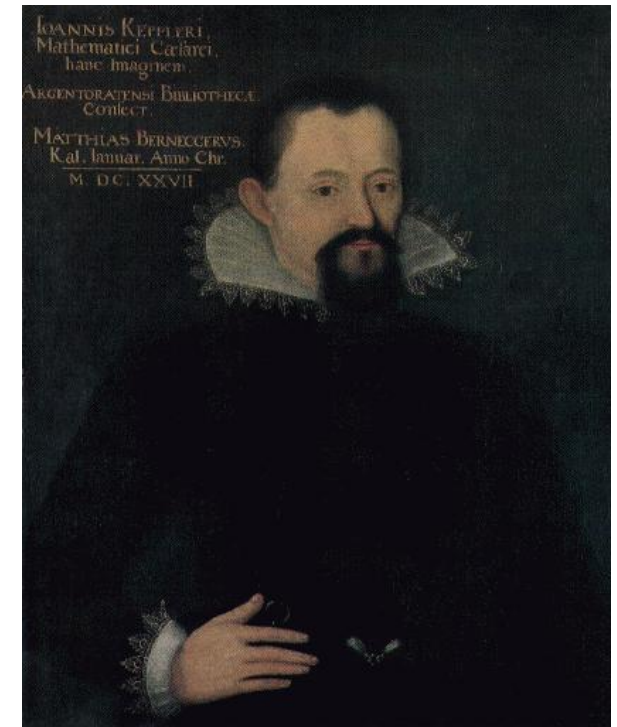


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Meeus (1989), Maor (2000)

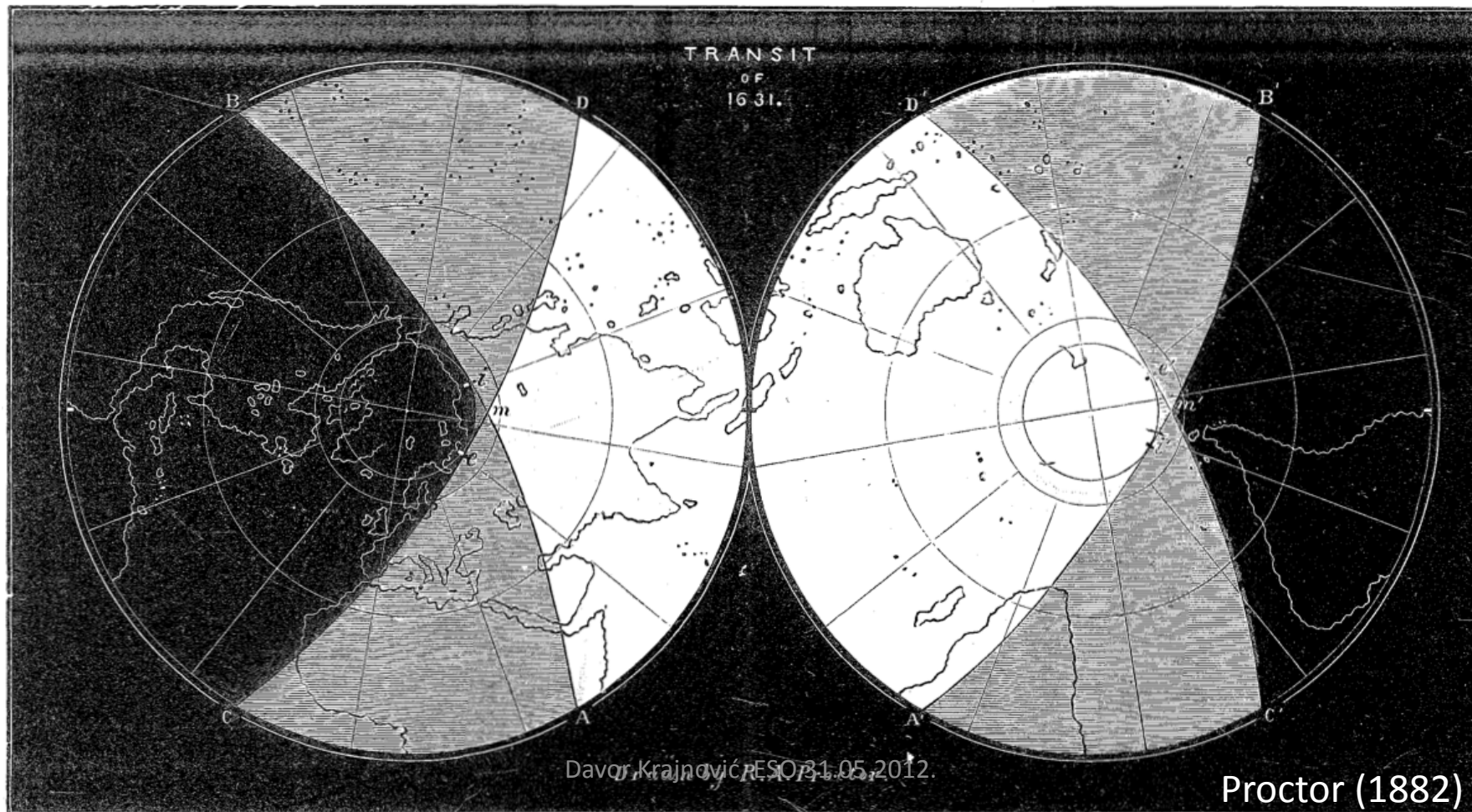
The prediction

- Johannes Kepler (1571 – 1630):
“Rudolphine tables”, 1627
 - Astronomical rules for finding Sun, Moon, planets
 - 1000 star coordinates (Brache’s observations)
 - Tables of logarithms
 - Geographical coordinates of major cities
- Two predictions:
 - Transit of Mercury: 7.11.1631
 - Transit of Venus: 6.12.1631



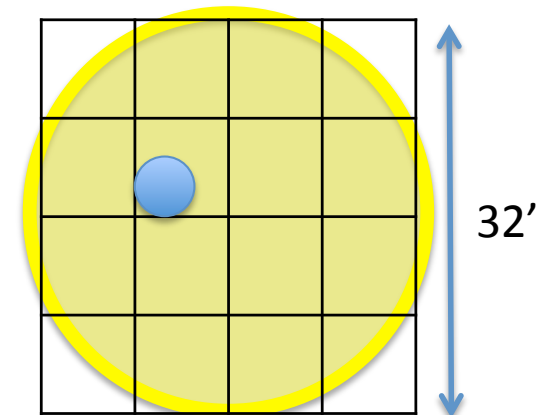
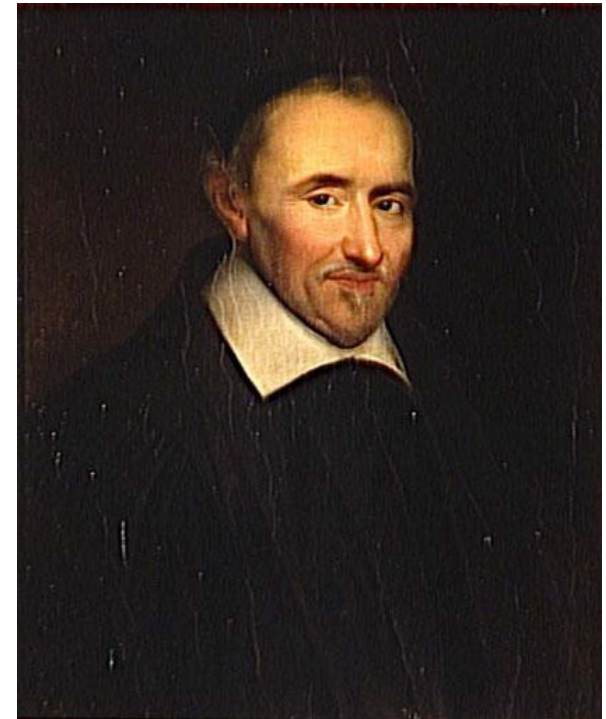
The first attempt on Venus

- Kepler predicted it would not be seen in Europe and issued a call “to mariner and learned men of the New World”



The first sighting of a transit

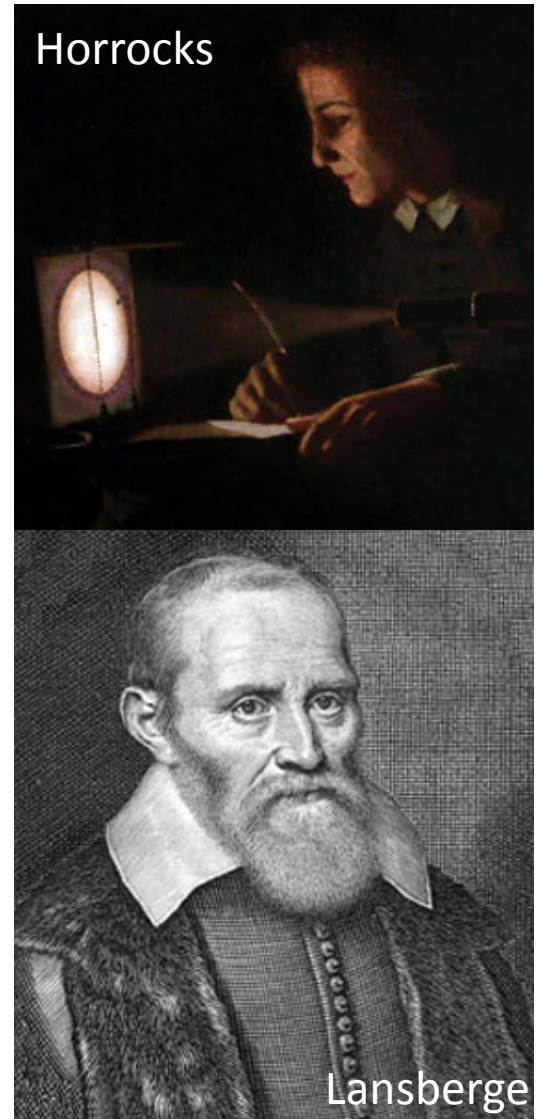
- 1631 transit of Venus is not recorded to be seen, but it was attempted
- Pierre Gassendi (1592-1655)
 - prepared for the transit of Venus, but it was cloudy from 4-6.12 and clear on 7.12 (too late)
 - “successfully” observed transit of Mercury in 1631
 - Through clouds: saw a dot on Sun, clouds came and went, the dot moved!!
 - measured apparent size of Mercury: 20''
 - Attempted to measure times of ingress and egress, but no good clocks available (used position of the Sun)



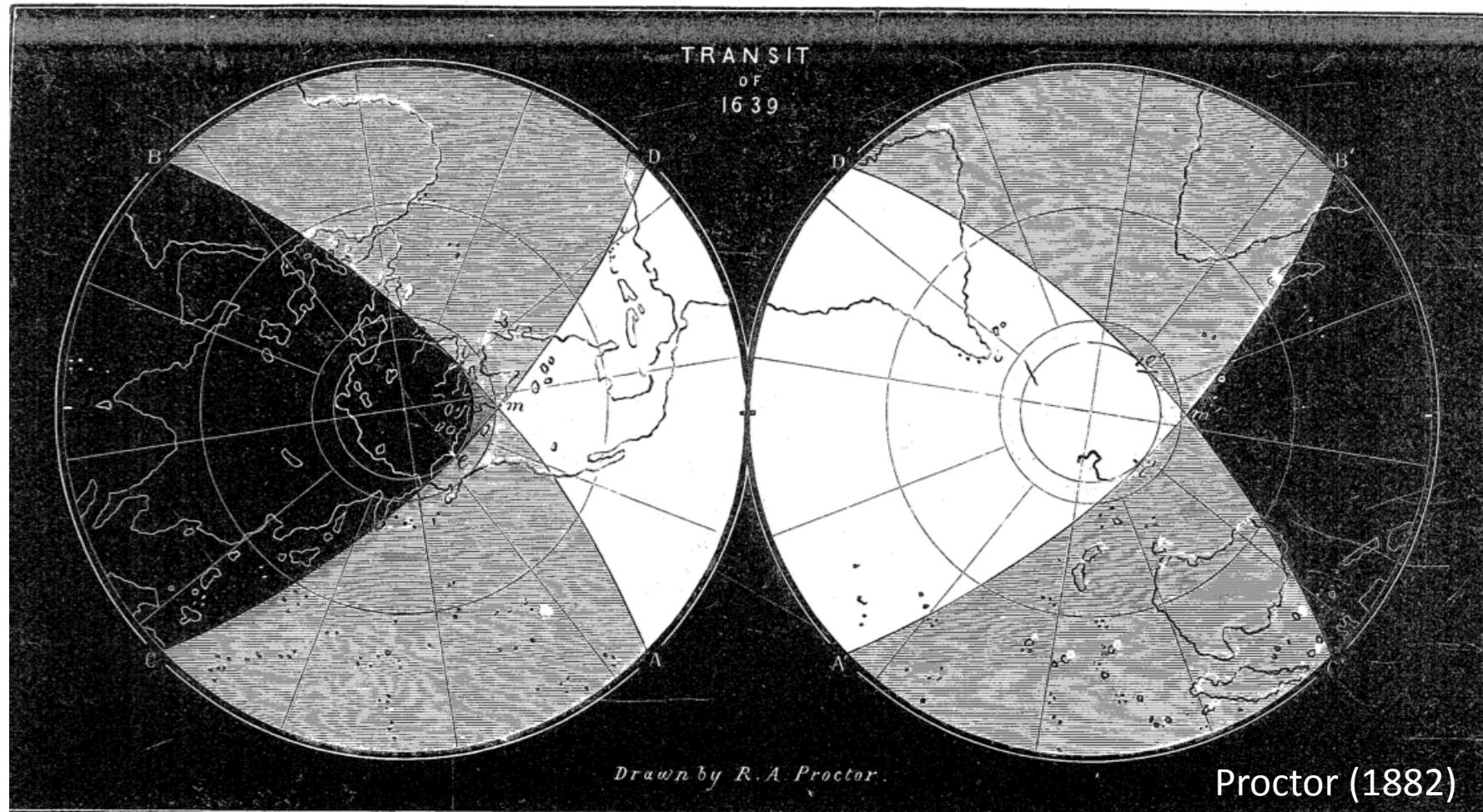
Unexpected second chance!

- Jeremiah Horrocks (1618-1641)
 - expert in Keplers theory of elliptical orbits (calculated the correct orbit of the Moon)
 - examined Rudolphine tables and calculated* that another transit will happen on 04.12.1639.
 - Confirmed using Lansberge tables (actually much worse than Rudolphine tables)

* Apparently it took him 3 years to calculate this, completed a month before the transit!



Visibility of the 1639 transit



Venus - ho!

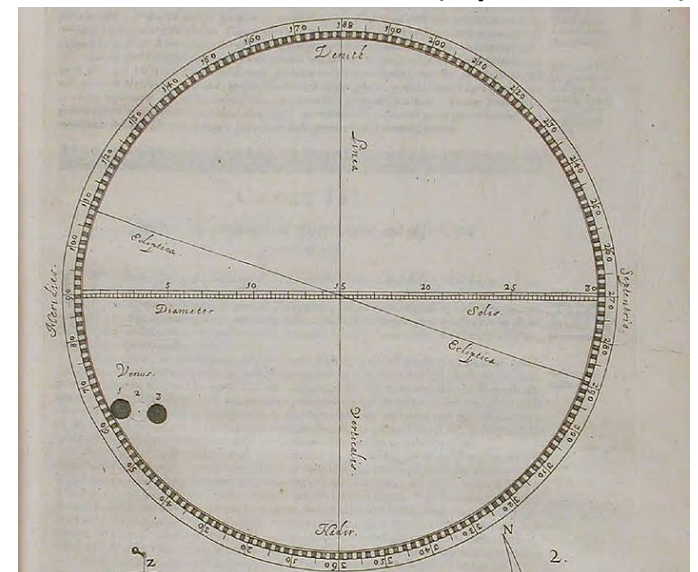
- Horrocks' prediction: Venus transits on 04.12.1639
- Started observing on 03.12.
- December 4, Sunday, Much Hoole
 - Observed since 10:00, cloudy
 - At 13:00 interrupted by “business of the highest importance”
 - Resumed observations at 15:15
 - No clouds at all
 - Venus on the Sun disc!
 - Sun set at 15:50
- Science:
 - Venus apparent size: $\sim 1'$ (much smaller than thought)
 - Confirmation of Kepler laws
- Died just after completing “*Venus in Sole Visa*”
- Publication of the results in 1662 by Johannes Hevelius as an Appendix to his book: “*Mercurius in Sole Visus Gedani*”

Davor Krajnović, ESO 31.05.2012.

Carr House where Horrocks observed (?) the 1639 transit

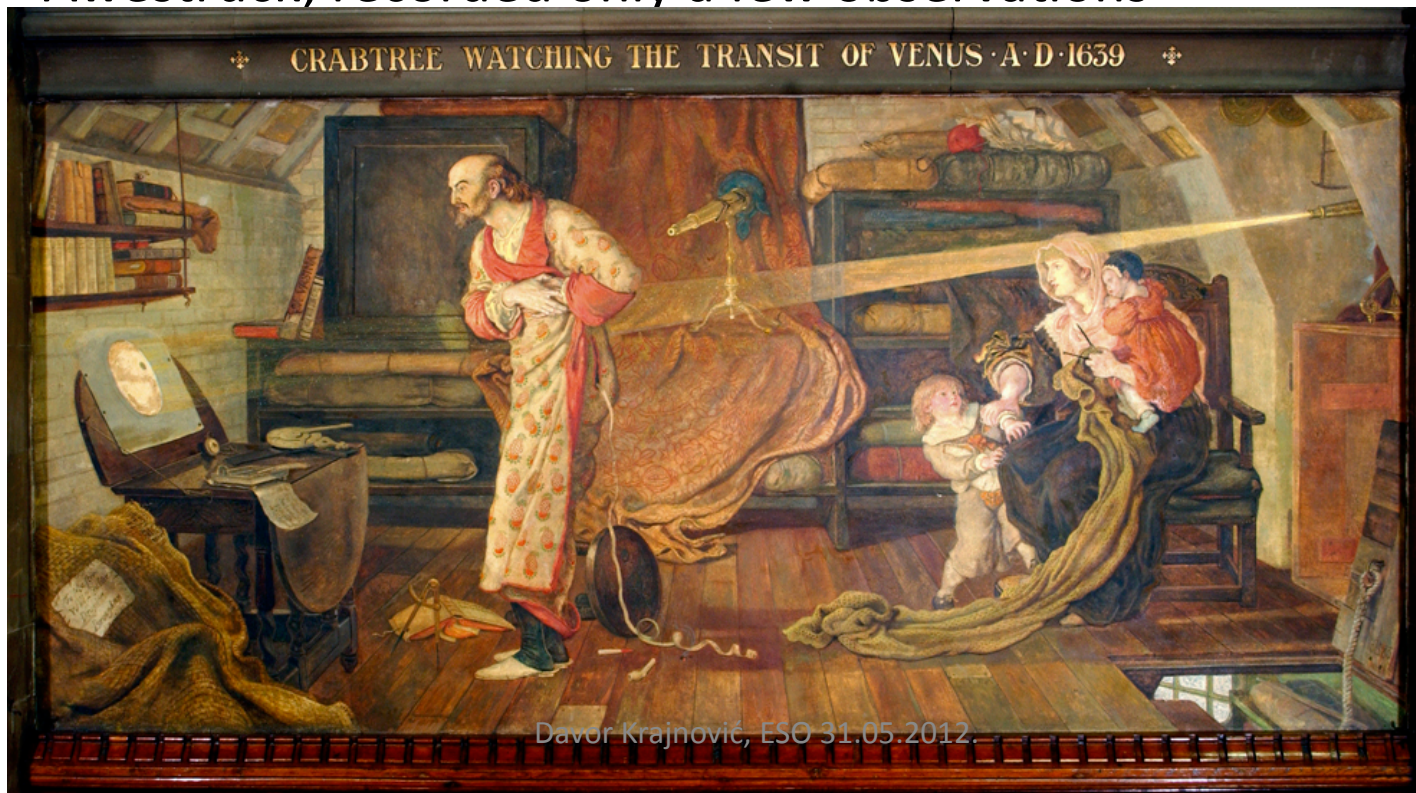


What Horrocks saw (by Hevelius)



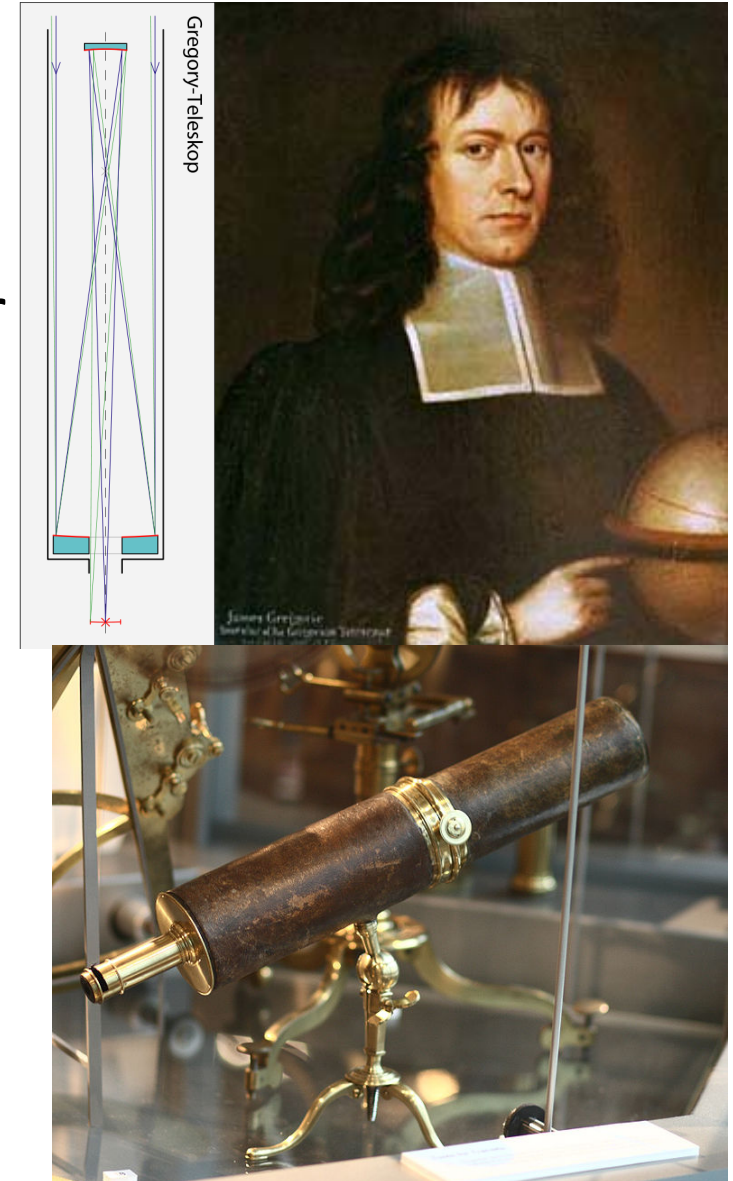
Only two men saw it!

- William Crabtree (1610-1644)
- December 4, Sunday, Manchester
 - Cloudy
 - 15:35 clouds disperse, Venus in sight!
 - Awestruck; recorded only a few observations



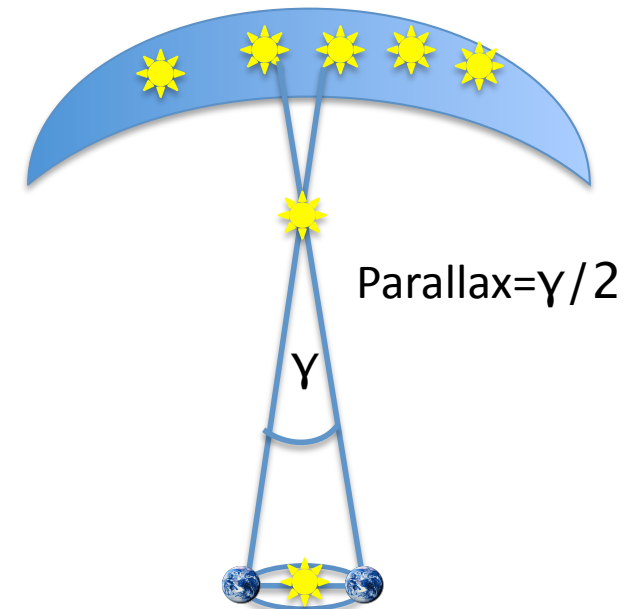
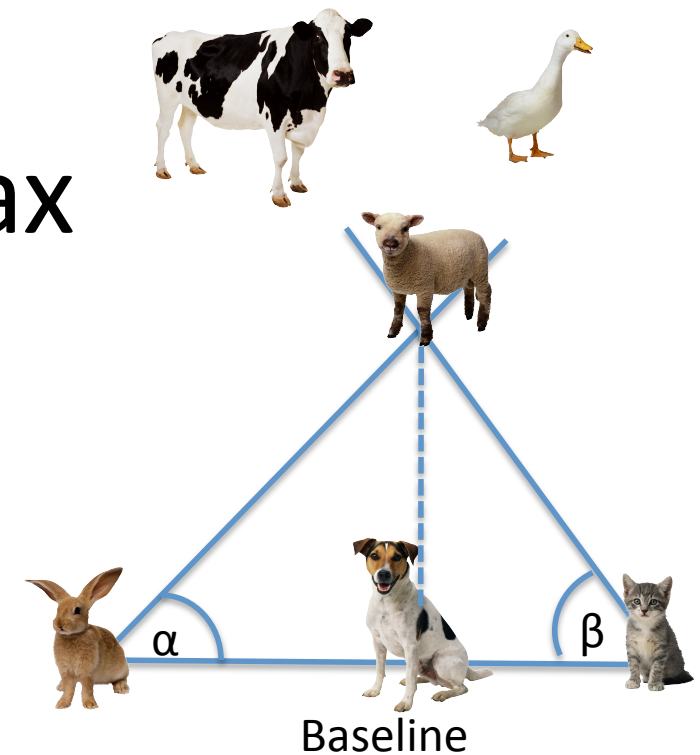
The measure of the Universe

- James Gregory (1638-1675)
- Optica Promota (1663)
 - suggested that transits of Venus or Mercury could be used to determine the **parallax of the Sun**
 - The Holy Grail of astronomy (and cosmology) – **DISTANCE**
 - **Period** squared is proportional to **distance** cubed: $P^2 \sim a^3$ (Kepler, 1616): $P_{\text{Earth}}^2 / a_{\text{Earth}}^3 = P_{\text{planet}}^2 / a_{\text{planet}}^3$



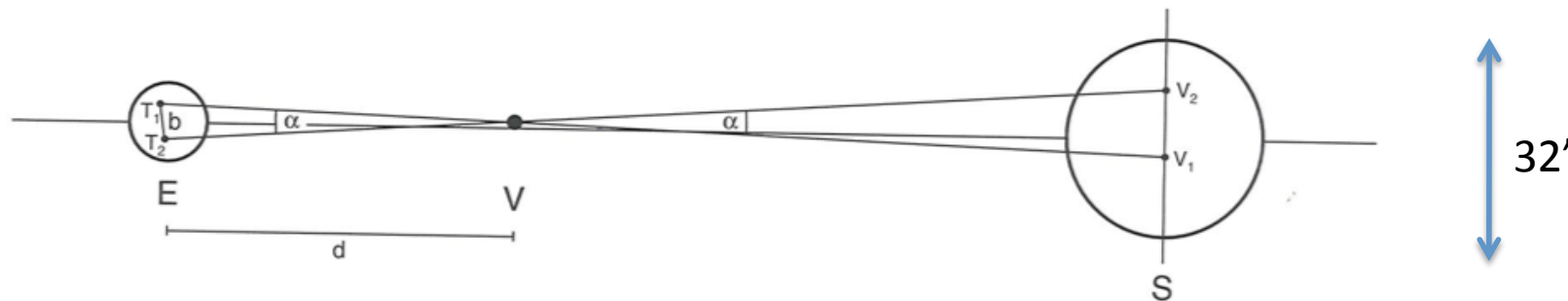
The method of parallax

- Used to measure the distance, from knowing angles in a triangle
- In astronomy: parallax = distance
- 1 parsec = distance to a star whose annual parallax is 1"
- Better accuracy for longer base line
- Hipparchus used Istanbul - Alexandria distance (~1000 km) to measure the parallax of the Moon
- Diameter of the Earth's orbit: parallax of stars (Bessel 1838 – 61 Cygni – 0.28")
- Diameter of Earth ~ 12000km
 - long enough to get the **parallax of the Sun** (or the distance Earth-Sun)
 - but can't see background!
 - can we use something else?



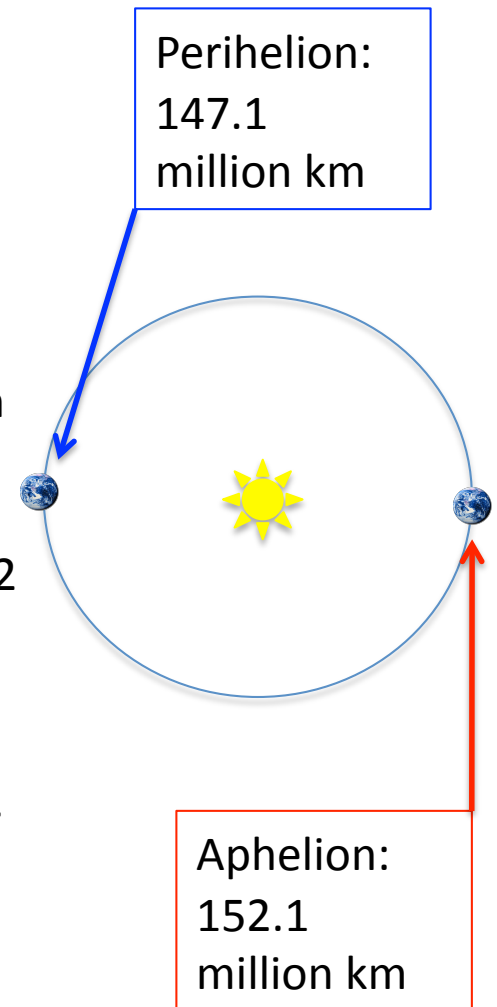
Solar parallax via parallax of Venus

- Send one astronomer to a place T_1
- Send another astronomer to a place T_2
- Let them measure the respective positions of Venus on the solar disc V_1 and V_2
- Compare with the diameter of the Sun to get α (knowing b) $\rightarrow d$
- From d and Kepler's 3rd law: distance to the Sun: **astronomical unit**
- Simple but:
 - Simultaneous observations needed!
 - Hm.... XVIII century



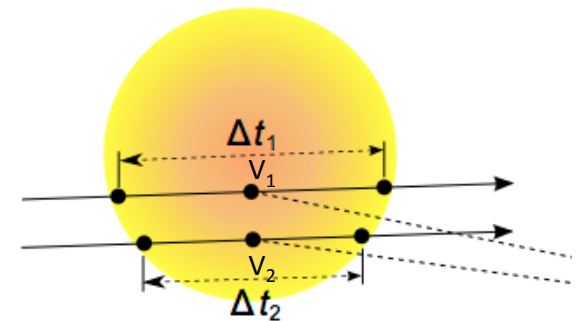
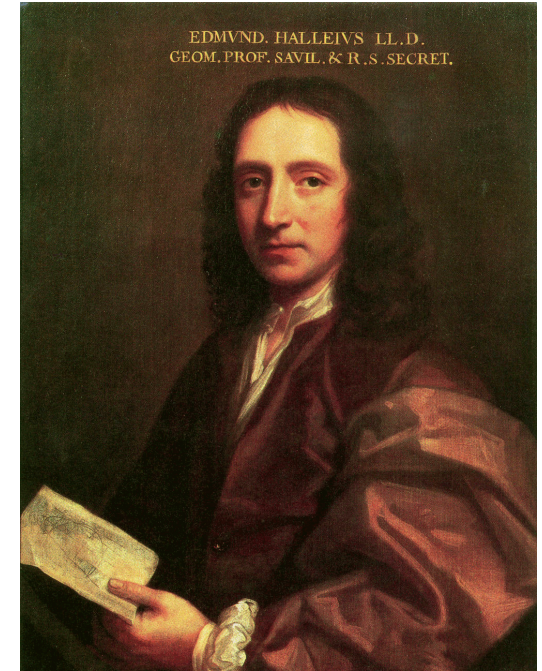
Astronomical Unit

- Originally defined as the length of the semi-major axis of the Earth's elliptical orbit around the Sun
- Today (IAU 1976 Grenoble): "The astronomical unit of length is that length (AU) for which the Gaussian gravitational constant (k) takes the value $k=0.017\,202\,098\,95$ when the units of measurement are – the astronomical units of length, mass and time."
- $k = \sqrt{GM}$, in the system where **mass** is in solar masses, **time** in mean solar day, and **length** is an AU.
- Alternatively: radius of a circular orbit around the Sun of a mass-less particle moving at an angular frequency of $0.017\,202\,098\,95$ radians per day, or a period of 365.2568983 days (known as a Gaussian year)
- Equivalent to 149 597 870 km
- Radar measurements or telemetry from space probes (to inner planets)
- **1 AU = 149 597 870.691 ± 0.03 km**
- Solar parallax: **8.794148** seconds of arc



Halley's method

- Edmond Halley (1656-1742)
 - Fellow of the Royal Society, Savillian Professor of Geometry, Astronomer Royal, Captain of the Royal Navy...
- Proposed a new method
 - *Methodus Singularis Qua Solis Parallaxis Sive Distantia a Terra, ope Veneris intra Solem Consipiciendoe, Tuto Determinari Poterit: Proposita Coram Regia Societate ab Edm. Halleio J.U.D. Ejusdem Societatis Secretario*, Phil. Trans., Vol. 29, 454, 1714-1716.
 - Instead of angle, let's measure the **duration** of the passage
 - Send astronomers to T_1 and T_2
 - Let them measure the durations of transit Δt_1 & Δt_2
 - Different durations \rightarrow different path lengths
 - Circle geometry \rightarrow angular distance between V_1 and V_2 = Venus Parallax
- Halley estimated accuracy of 1 sec or 1/500 for the distance



Delisle's improvement

- Joseph Nicolas Delisle (1688 – 1768)
- Improvement (1743):
 - (only) record the timing of the ingress and/or egress (t_{1i} , t_{2i}), (t_{1e} , t_{2e})
 - $t_{1i} - t_{2i} \sim \Delta t_1 - \Delta t_2$
 - easier to measure (less dependant on weather) + partial sites also included
- Halley: call for action
- Delisle: spiritus movens:
 - Mobilised and prepared the scientific community
 - Produced the Mappemonde for 1761 transit



An astronomical challenge

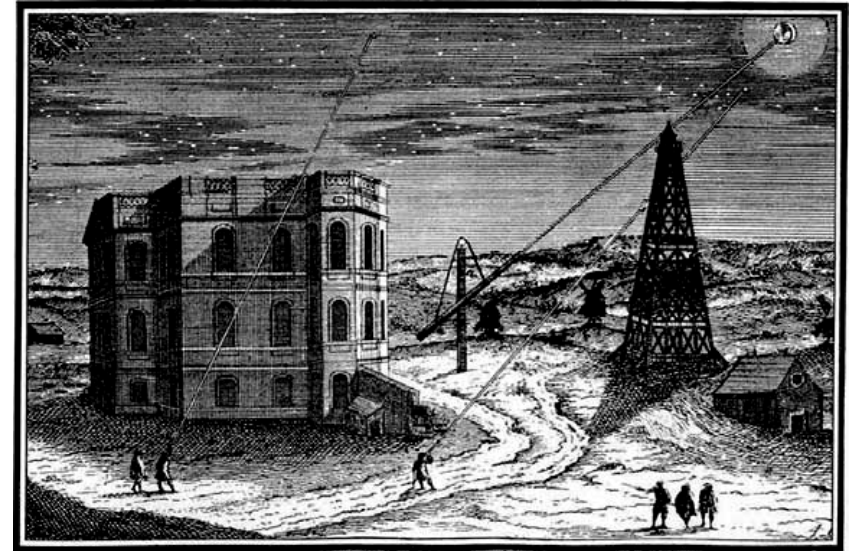
- Challenges:
 - **Longitudes** are not well known and difficult to determine
 - **Clocks** are only partially good time keepers
 - **Travelling** is very expensive and very long
 - Only 1 previous transit recorded!
- Results can be achieved only via organised scientific expeditions
- Role for the learned societies



H4 – Harrison Chronometer
1759.
Affordable chronometers
from 1783.

Change of World

- Many things happen in 120 years
- Science became a respectable occupation (for those who could afford it)
- Scientists considered as useful people
- Paris Observatory (1667)
- Greenwich Observatory (1675)
- Leopoldina (1652)
- Royal society (1660)
- Académie des Sciences (1666)
- The Republic of Letters
- The spirit of the Enlightenment
 - There is interest (to spend money) for understanding natural phenomena
 - There is a conviction the natural world can be explained



Paris (above) and Greenwich (bellow)
Observatories



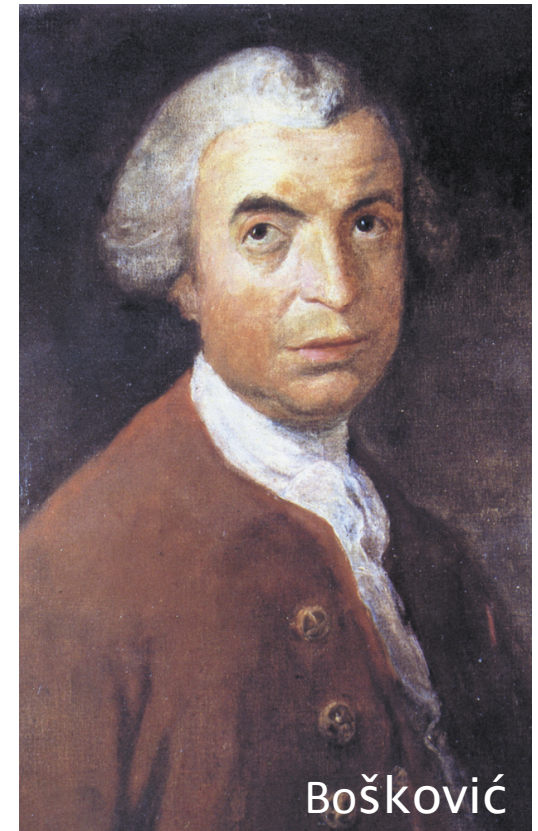
The French

- Local observations:
 - Paris Observatory – Maraldi
 - Palais du Luxembourg – Lalande
 - Observatoire de l'Ecole Militaire – Jeaurat
 - Observatoire de la marine - Messier
 - Hote de Cluny – Lemonnier/La Condamine + Louis XV
- Académie des Sciences – several expeditions
 - Chappe d'Auteroche – Tobolsk
 - Pingré– Rodrigues Island
 - Le Gentil de la Galaisiere – Indian Ocean
 - Cassini de Thury – Vianna, Austria



The British

- Hm.... Not really prepared
- On June 19. 1760 a paper was read by a visiting Jesuit (a Croatian!) at the Royal Society: R. Boscovich, *De Proximo Veneris Transitu* (Phil. Trans. 1759, 51, 865)
- His points why should RS organise expeditions:
 - (Measurement of the solar parallax)
 - Its famous member (Halley) devised the method
 - England is the best in making astronomical instruments
 - English astronomers always made significant discoveries
 - French are preparing several expeditions and English shouldn't be left behind!
- He brought the Delisle's Mappemonde
- Action:
 - Nevil Maskelyne – St. Helena
 - Charles Mason & Jeremiah Dixon – Sumatra
 - Several local observations

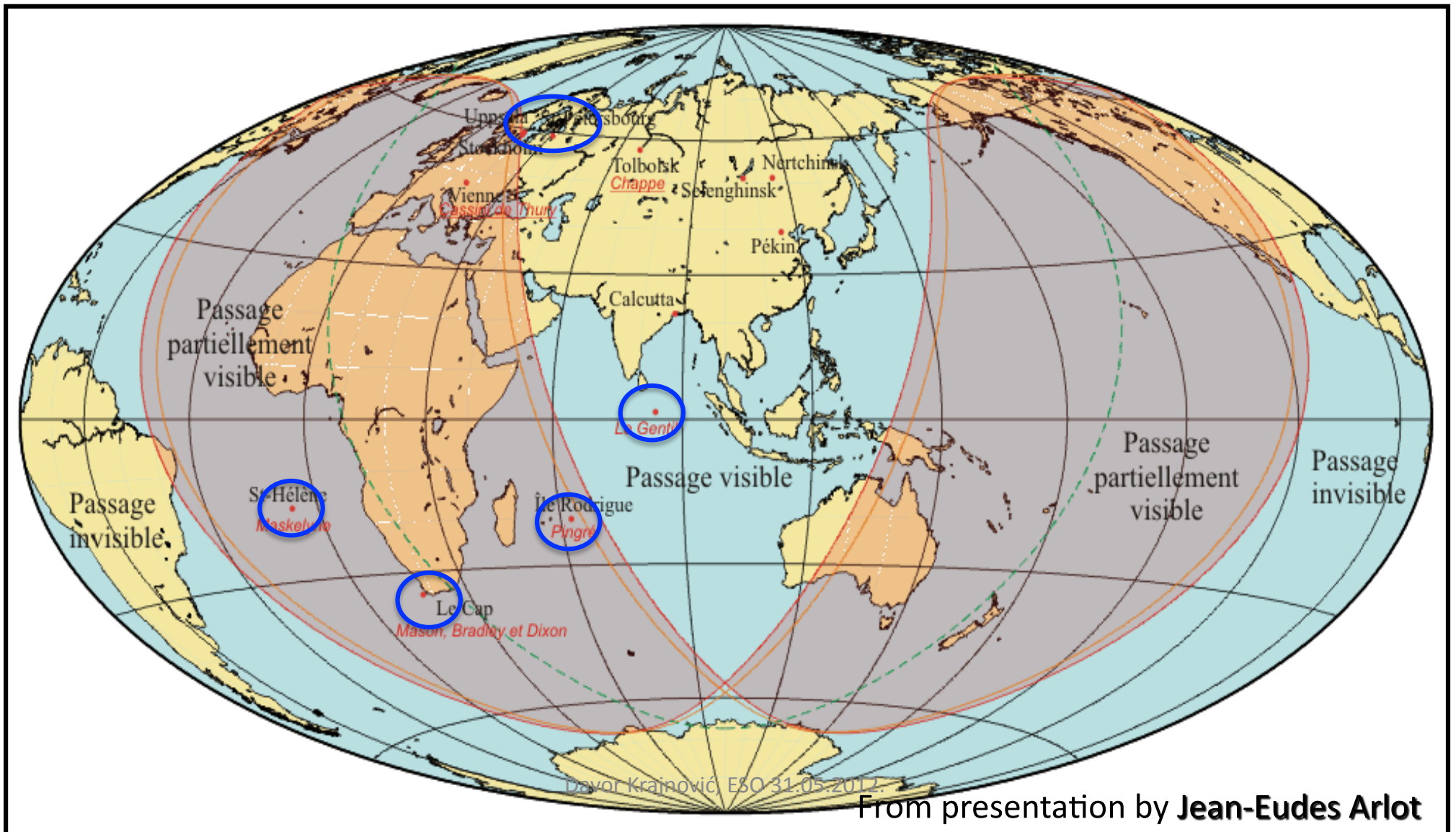


The seven years war (1756-1763)



- Global conflict between Britain and France

Observations of 1761



Pingré

- Alexandre – Gui Pingré (1711-1796)
 - Rodrigues Island
 - Rain and clouds, windy
 - No useful observations!
 - While on Rodrigues: island twice sacked by British
 - On the way home: attacked and captured by a British warship which dropped him off in Lisbon
 - His conclusion: *“Liquor gives us the necessary strength for determining the distance of the Earth from the Sun.”*



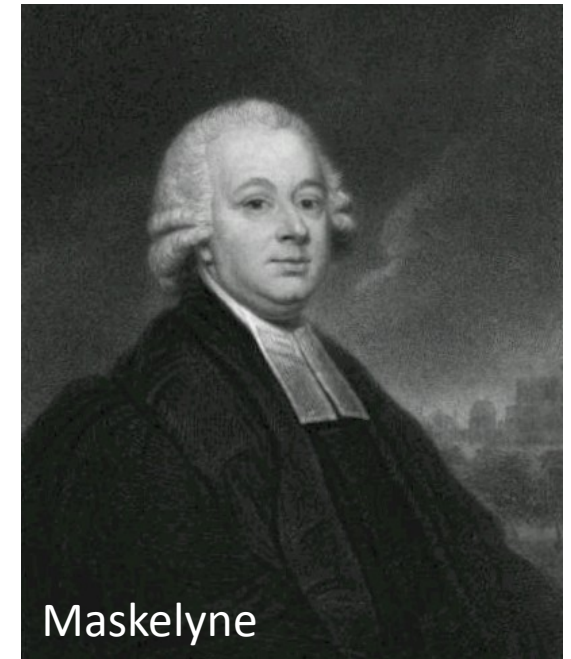
Le Gentil

- Guillaume-Joseph-Hyacinthe-Jean-Baptiste Gentil de la Galaisière (1725- 1792)
- Pondicherry, India
- Slow passage due to no wind on frigate *La Sylphide*
- Reached India on 24.05
- News: Pondicherry fallen to British
- Captain turned the frigate around
- Observed on the boat:
 - Clear skies
 - And a shaky boat....
- Not demoralised: decided to stay in the Indian Ocean and wait for the next transit!
- Studied local flora and fauna
- Stay tuned....



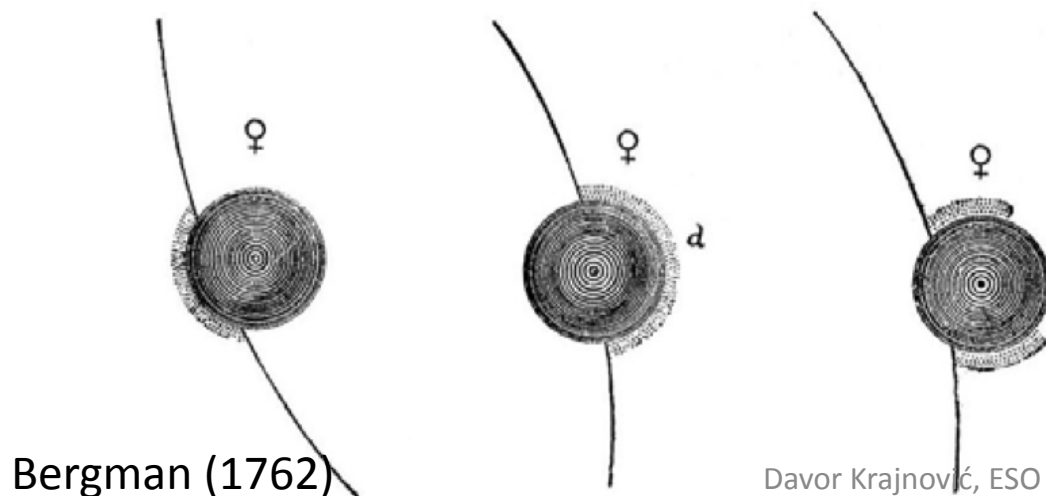
Maskelyne & Mason

- Nevil Maskelyne (1732 – 1811)
 - Future Astronomer Royal
 - St. Helena
 - Cloudy
 - Useful study of sea currents and tides
- Charles Mason (1730-1787)
 - Destination: Sumatra
 - Left Portsmouth on *HMS Sea Horse*
 - Attacked by a French frigate in the Channel
 - Returned and refused to go again!
 - Forced to leave again
 - Went as far as Cape of Good Hope (Sumatra fallen to French)
 - Good weather → the only successful observations in the south!

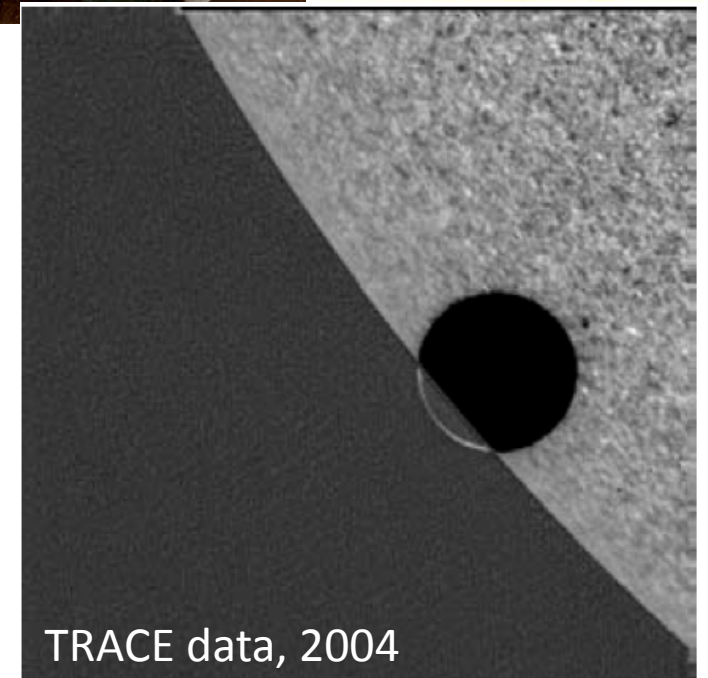


Lomonosov & Bergman

- Mikhail Vasilyevich Lomonosov (1711- 1765)
 - St. Petersburg
- Tober Olof Bergman (1735- 1784)
 - Uppsala
- Discovery of Venus Atmosphere
 - Lomonosov (1761a,b)
 - Bergman (1762, Phil.Trans. 52, 227)



Davor Krajnović, ESO 31.05.2012.



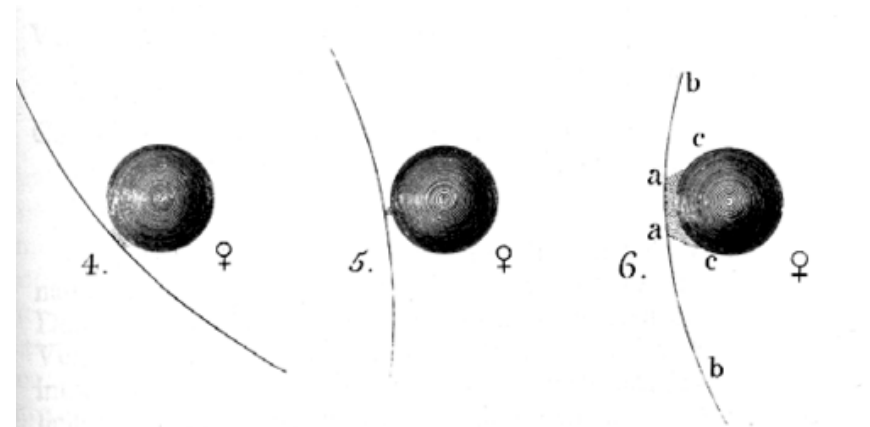
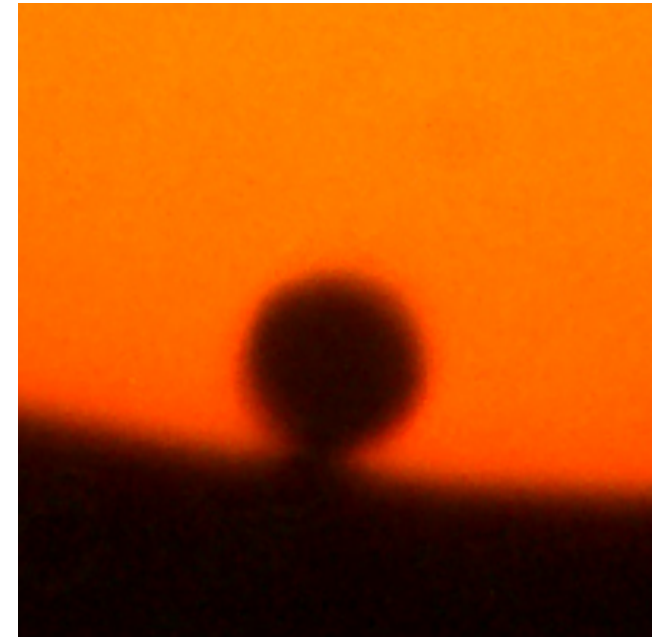
Results of 1761

- 120 observers at 62 separate locations
- Estimates for Solar parallax:
 - 8.5'' – 10.5''
 - Or 1 AU = 125 100 000 - 154 600 000 km
 - (Halley expected an error of ~300 000 km)
- Overall disappointing
- Bad weather and inexperienced of astronomers
- **Not precise longitudes**
- **The black drop effect!**
- The second chance is only 8 years away and now astronomer will be prepared!!

1 AU TODAY:
8.794148''
149 597 870 km

The black drop effect

- Halley's and Delisle's methods dependant on precise measurement of entry and exist of Venus
- Observers expected a sudden separation of Venus and Sun's limb, but
- Venus' trailing edge seemed to linger on
- Instead of 1-2 sec timing accuracy, observers were not able to decide when is Venus in the disc of Sun to 10 sec or more!

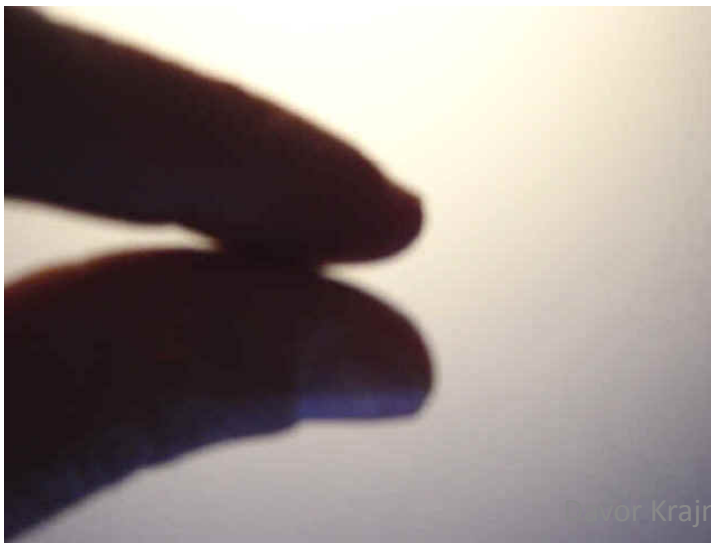
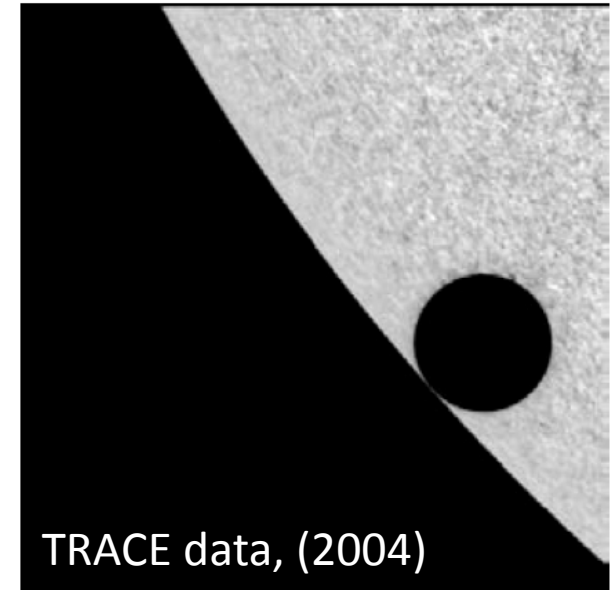


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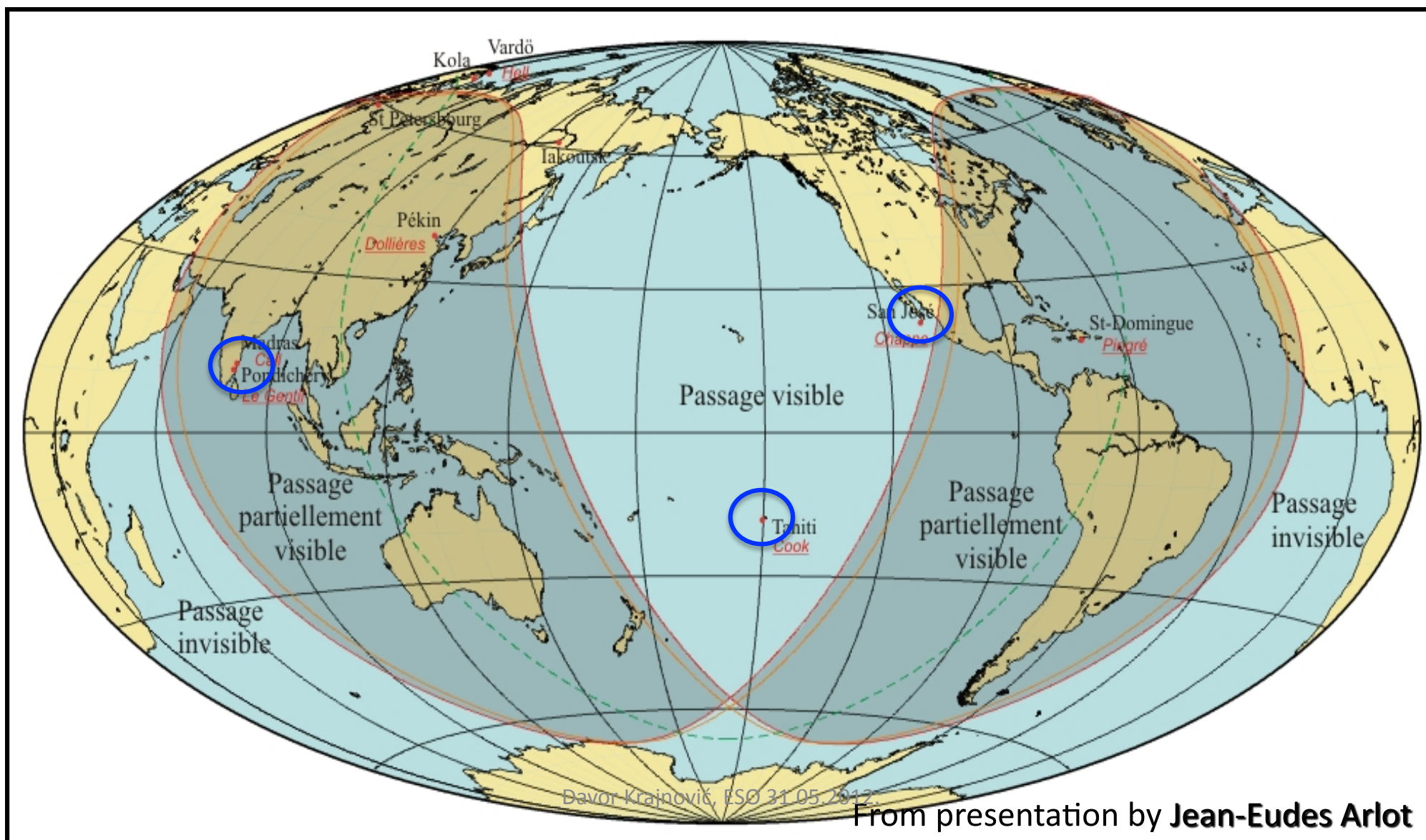
Bergman (1762)

The black drop explained

- Combination of:
 - (Venus atmosphere)
 - Earth atmosphere
 - Optical effect of a bright background
 - Instrumental effects !!!
- Once a pest, today a prize (but not seen often!)



Voyages of 1769



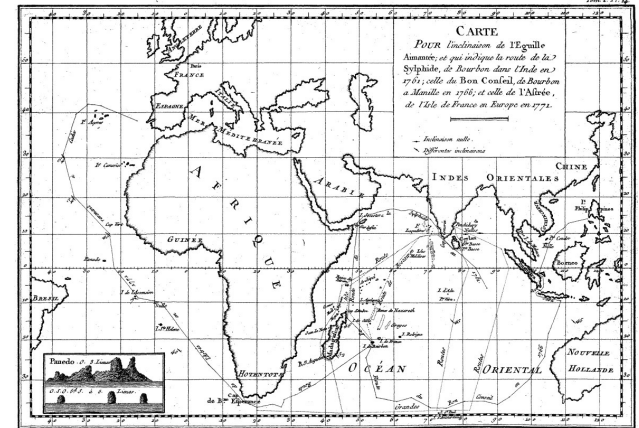
d'Auteroche

- Abbé Jean-Baptiste Chappe d'Auteroche (1728-1769)
 - Solomon Islands (then under Spain)
 - Not allowed → sent to Mexico (boat to Veracruz, overland to southern tip of Baja California)
 - Jose del Cabo (16.05.1769)
 - Great weather, one of the most precise measurements
 - Before departure: epidemic broke in the village
 - Most of the inhabitants died
 - Only one survivor of the expedition: geographer M. Pauly – brought back the data
 - *“Voyage en Californie, pour l'observation du passage de Vénus sur le disque du soleil”*, published by Cassini de Thury



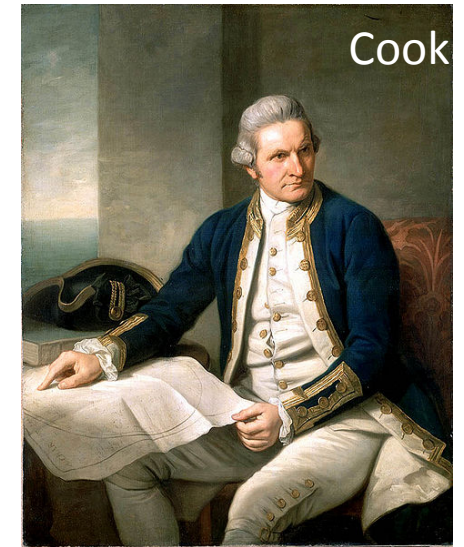
Le Gentil – record for astronomical persistence

- Stayed on Mauritius, travelled around the Indian ocean exploring wildlife and natural history
- Decided to go to Manila, Philippines
- Academy sent him back to Pondicherry
- (This time) British offered assistance (+ a telescope)
- On the day of transit: cloudy (in Manila sunny!)
- Mild nervous breakdown...
- Return home delayed due to dysentery and a shipwreck
- Upon return home:
 - Assumed dead by his family: estate plundered and divided
 - Academy “retired” him (as he must have neglected his duties for some personal benefit)
 - After a lengthy legal fight (and intervention by the King) got his property back
 - Got married and had a daughter
 - Published: *Voyage dans les mers de l'Inde, fait par ordre du Roi, à l'occasion du passage de Vénus, sur le disque du Soleil, le 6 juin 1761 & le 3 du même mois 1769, (1779, 1781)*

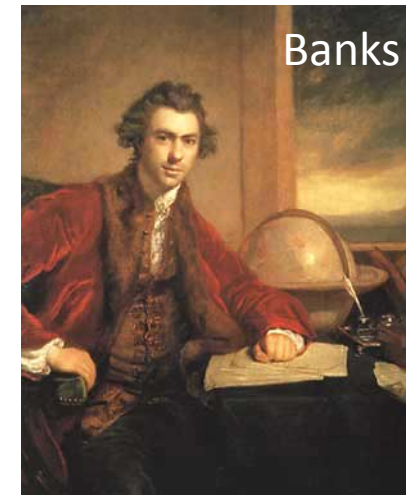


Cook

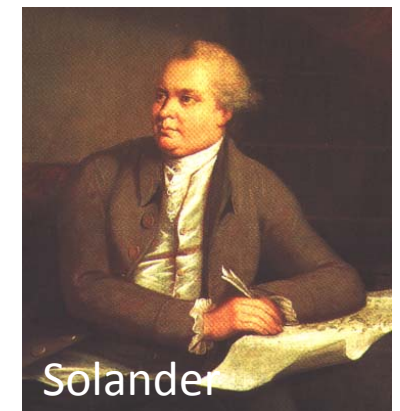
- Transit best visible from the South seas
- Uncharted (unknown) regions
- Interest in combining the astronomical and exploratory expeditions under the RN
- Lieutenant James Cook (1728 – 1779) and HMS Endeavour (built for coal trade)
- Scientists:
 - Joseph Banks, Esq (future President of the RS)
 - Charles Green, astronomer (1735 – 1771)
 - Daniel Solander, botanist (1733 – 1782)



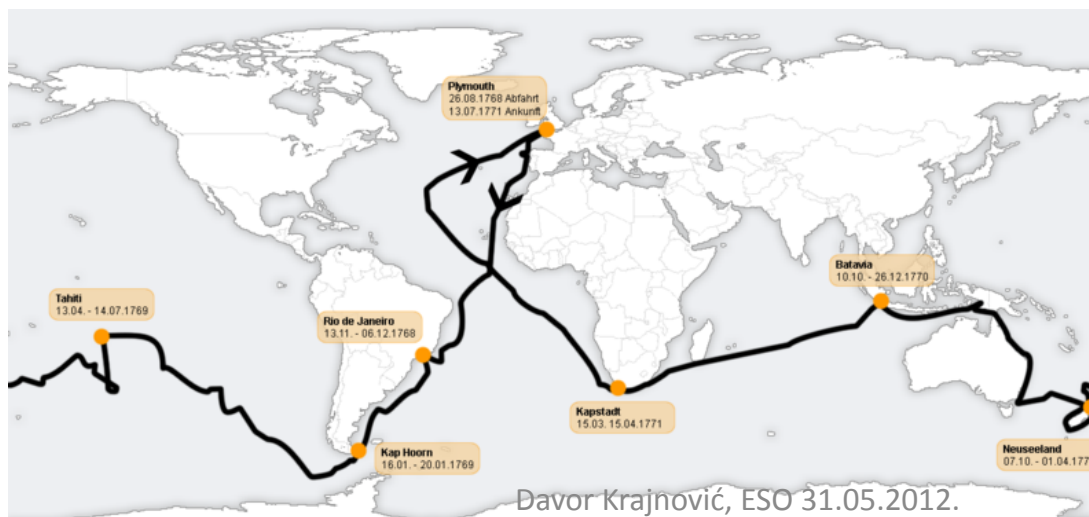
Cook



Banks



Solander



Cook's Venus Transit

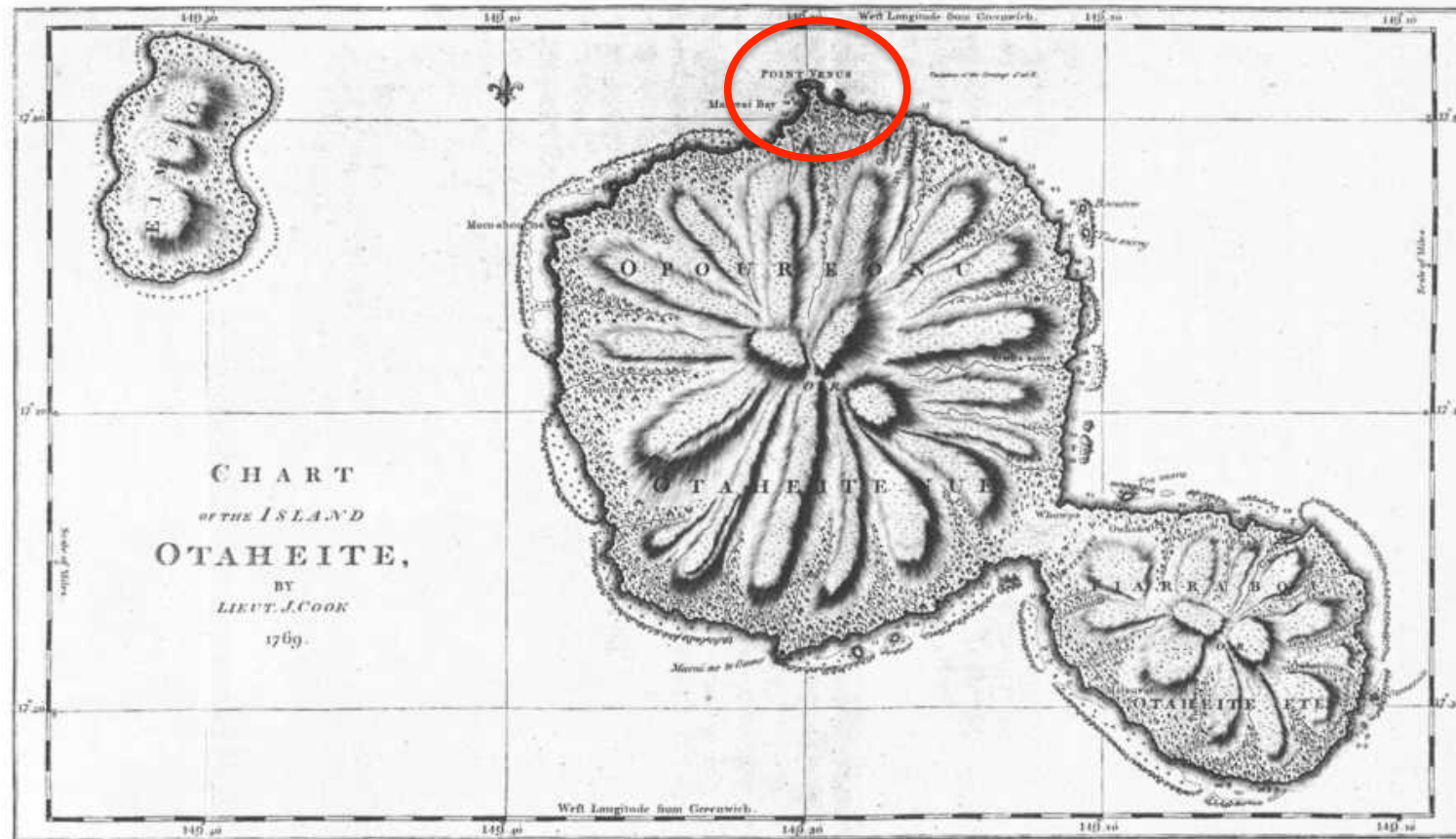


Fig. 4. Cook's chart of Tahiti, showing Matavai Bay and Point Venus (reproduced from Hawkesworth)

Cook's Venus Transit

- Tahiti - the only place in Pacific with known longitude and latitude
- Fort Venus
- Small trouble with natives
 - Stolen quadrant reassembled
- Clear skies and

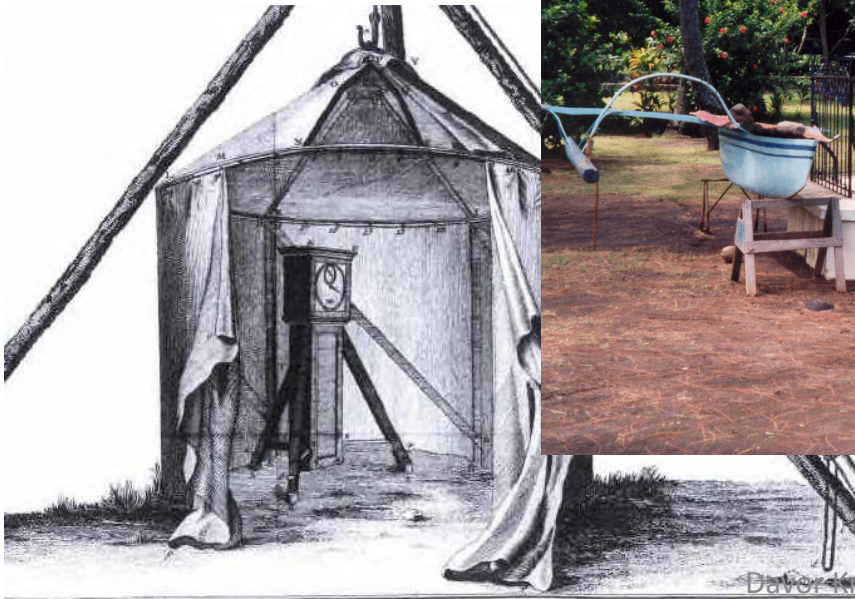
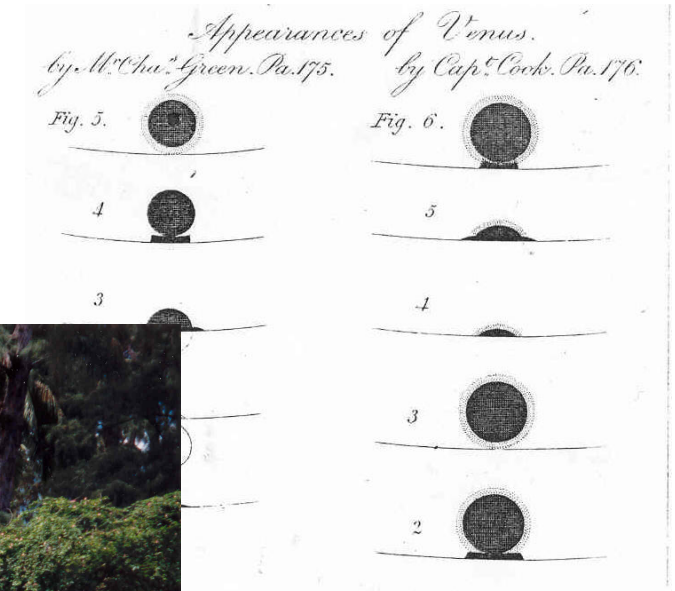
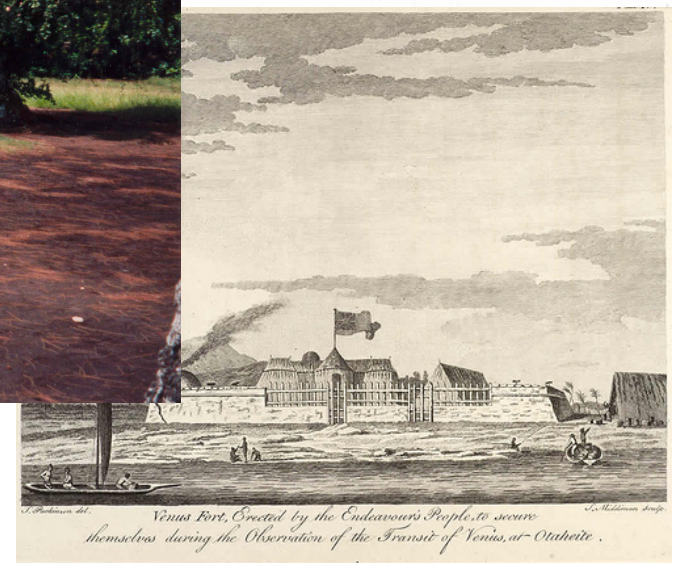


Fig. 1. Observatoire portatif. Fig. 2. Manière d'établir une Horloge Astronomique à terre.



Venus Fort, Erected by the Endeavour's People, to secure themselves during the Observation of the Transit of Venus, at Otaheite.

Results of 1769

- 138 observers at 63 locations
- Better results than in 1761:
 - Solar parallax: $8.43'' - 8.80''$
 - AU = 149 300 000 – 153 900 000 km
- But not as expected
 - Black drop (timing issue)
 - Uncertain longitudes
- RS escape goat: Charles Green (died during voyage)

1 AU TODAY:
 $8.794148''$
149 597 870 km

105.5 years later

- The world changes again
 - Industrial revolution
 - Faster and safer travels
 - Good time keepers
 - Determining longitude not a very big deal
 - Photography (daguerreotypes)
 - Lots of past experience
 - New nations (USA, Germany...) willing to prove themselves
- But is it necessary?
 - Precision in astronomy reached new levels: sub-arcsecond (e.g. Bessel in 1838 determined parallax of 61 Cyg of 0.28")
 - AU from the parallax of Mars



Fig. from presentation by
Jean-Eudes Arlot

Parallax of Mars

- Attempted before
 - Jean Richer (1630-1696) - Cayenne
 - Giovanni Cassini (1625 – 1712) – Paris
 - 1 AU ~ 190 000 000 km
 - Not sufficient precision in measuring angles, but possible in 19th century!

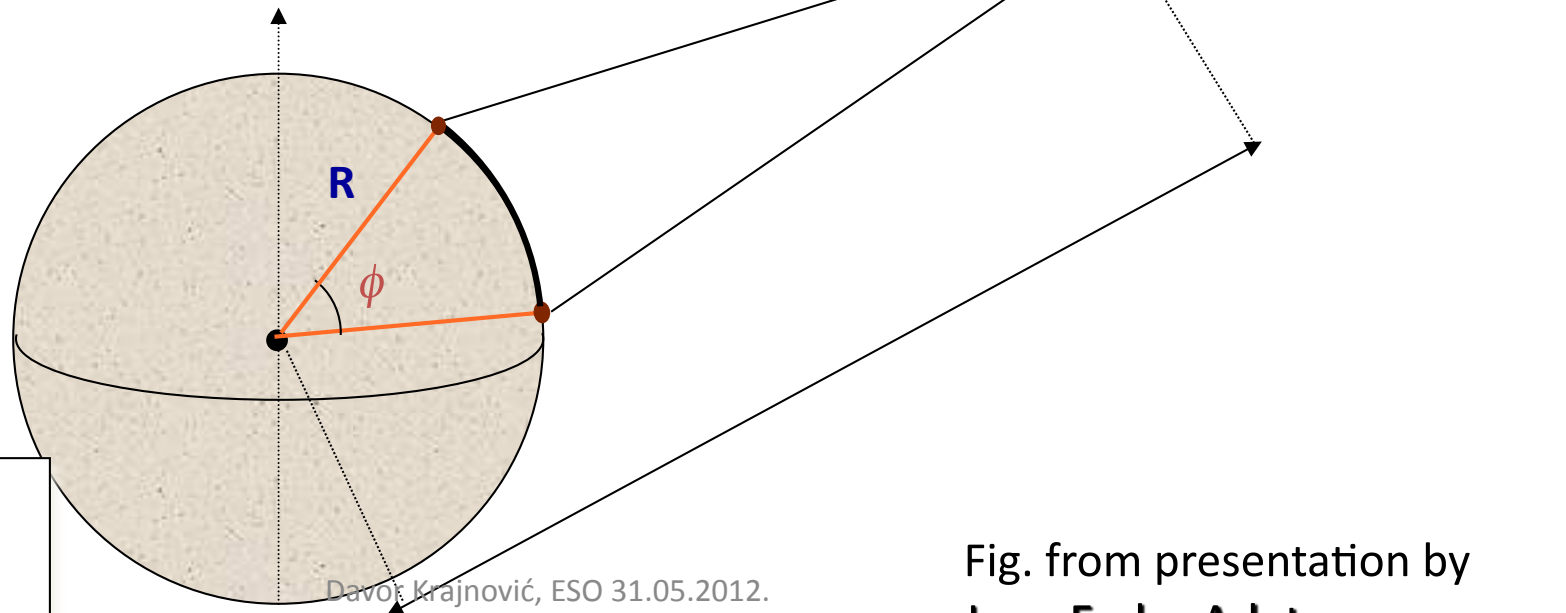
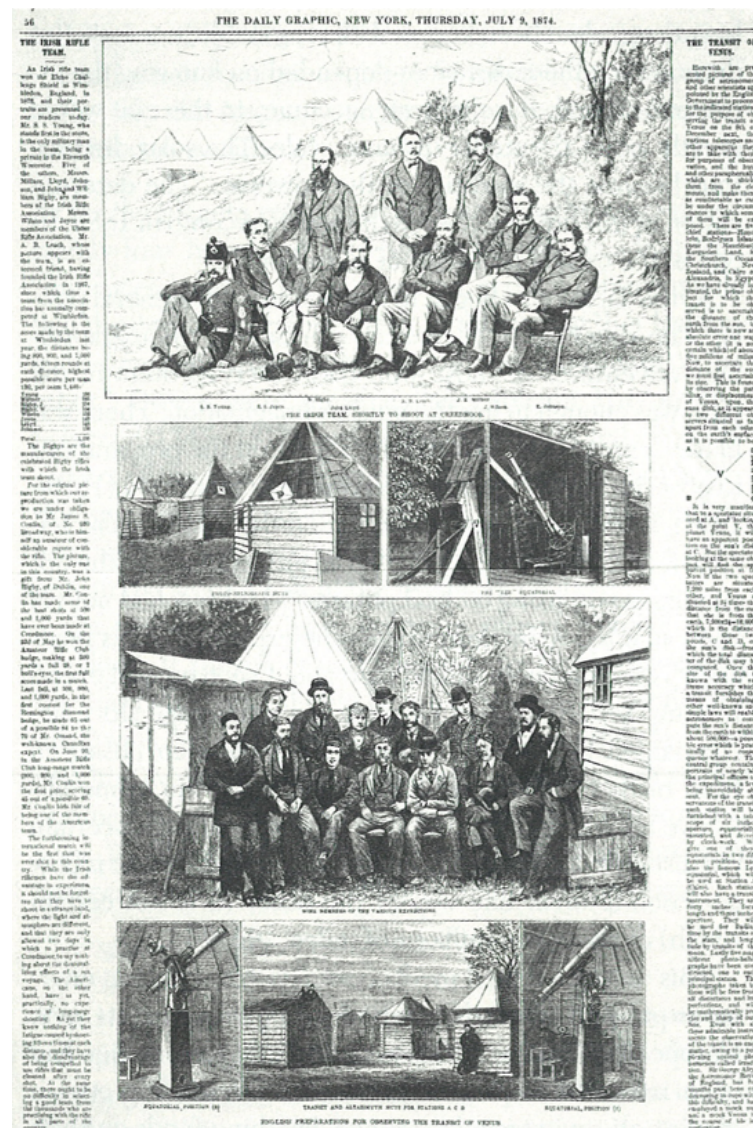


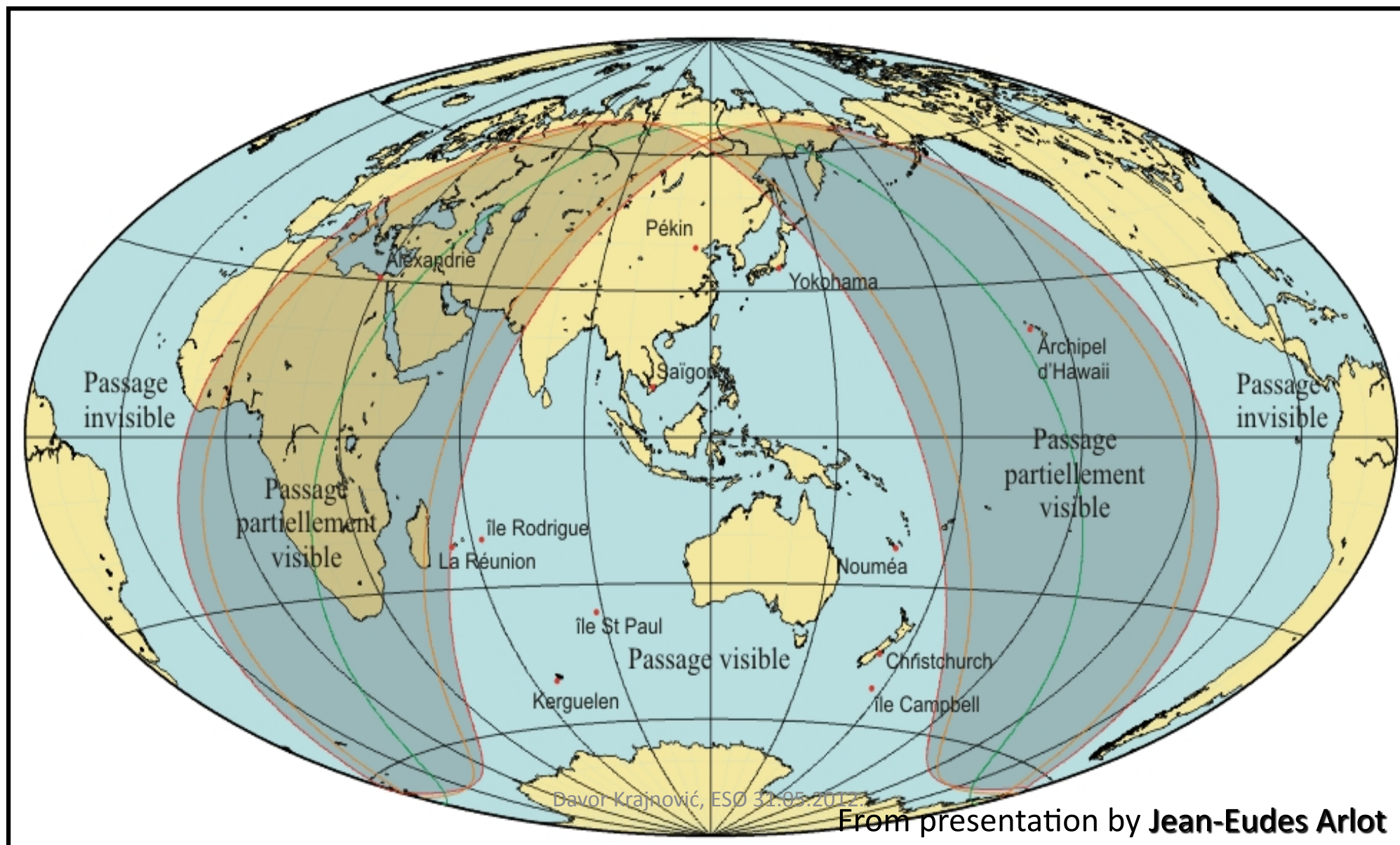
Fig. from presentation by
Jean-Eudes Arlot

No problem with money

- Venus transit still very attractive
- Media coverage
 - Rarity of the event + adventures of 18th century
 - All newspapers report on the progress of expeditions
- General public
 - Governments “happy” to spend money
 - US Congress (1874):
 - Approves \$50 000 (today: \$1.25 million)
 - Final sum: \$175 000 (today: \$4.375 million)
 - US Congress (1882)
 - Approves \$85 000 at start (even though some astronomer were against, including S. Newcomb – see later)
 - World wide (1874): > \$1 000 000 (today: 25 million)



Voyages of 1874

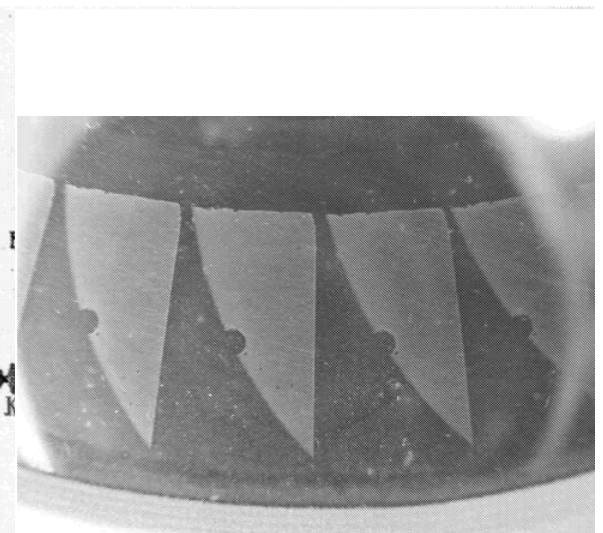
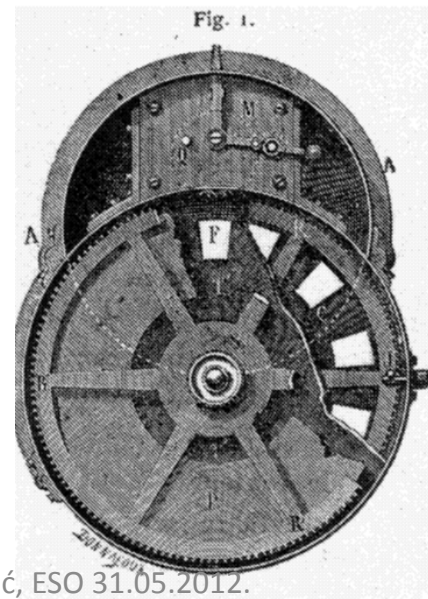
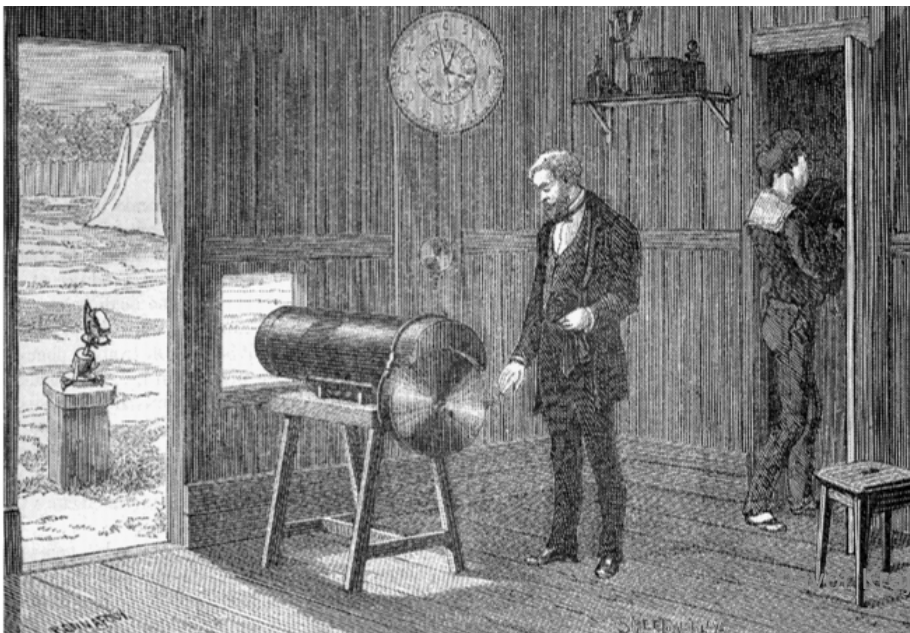


Expeditions

- French 1872: 2 north, 2 south
- British 1872: several
- *Conference internationale du passage de Venus* (1881) – Paris
 - Call for cooperation in selection of locations
 - Discussion of technical details (i.e. photography)
- British 1884: 16 teams at 6 locations
- France 1884: (at least) 8 locations
- Many, many other countries

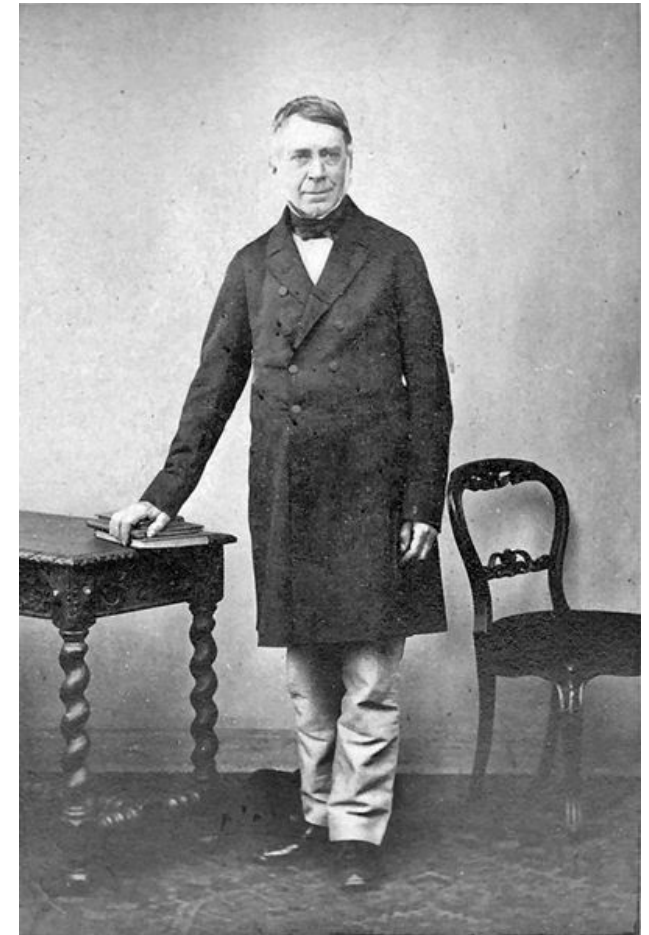
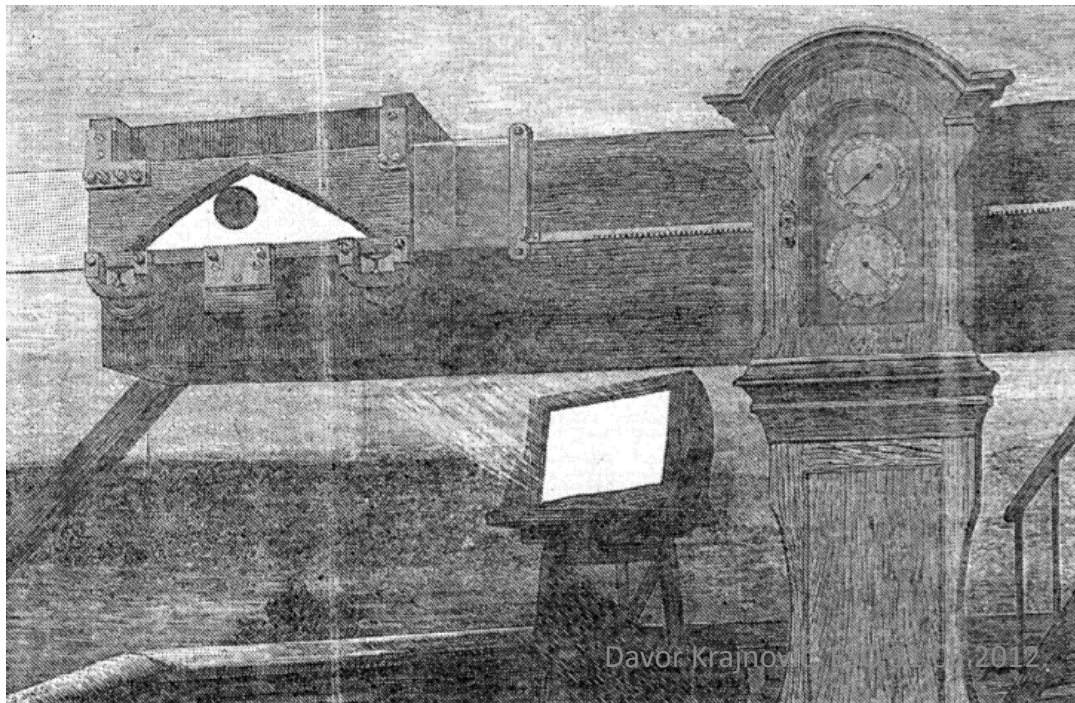
New technology

- Jules Janssen (1824-1907)
 - Observing in Japan
 - ‘revolver photographique’
 - Technology spin off: cinema



New approach

- George Biddell Airy (1801-1892)
 - Astronomer Royal
- Practicing for the Venus transit
 - Done by other nations as well
 - Systematic preparations of large team of scientists and support staff



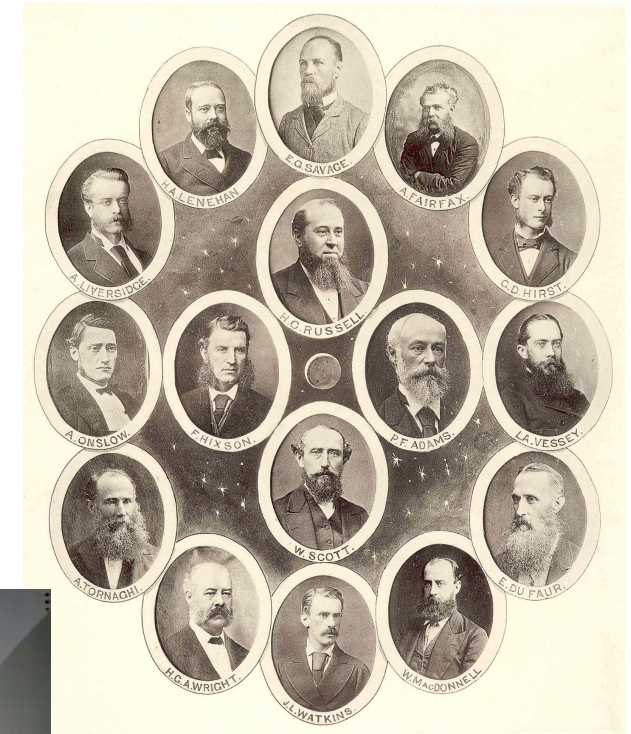
New homecoming

- Commemorating medallions
- Photographs
- Paintings

Medallion commemorating
1874 and 1882 transits

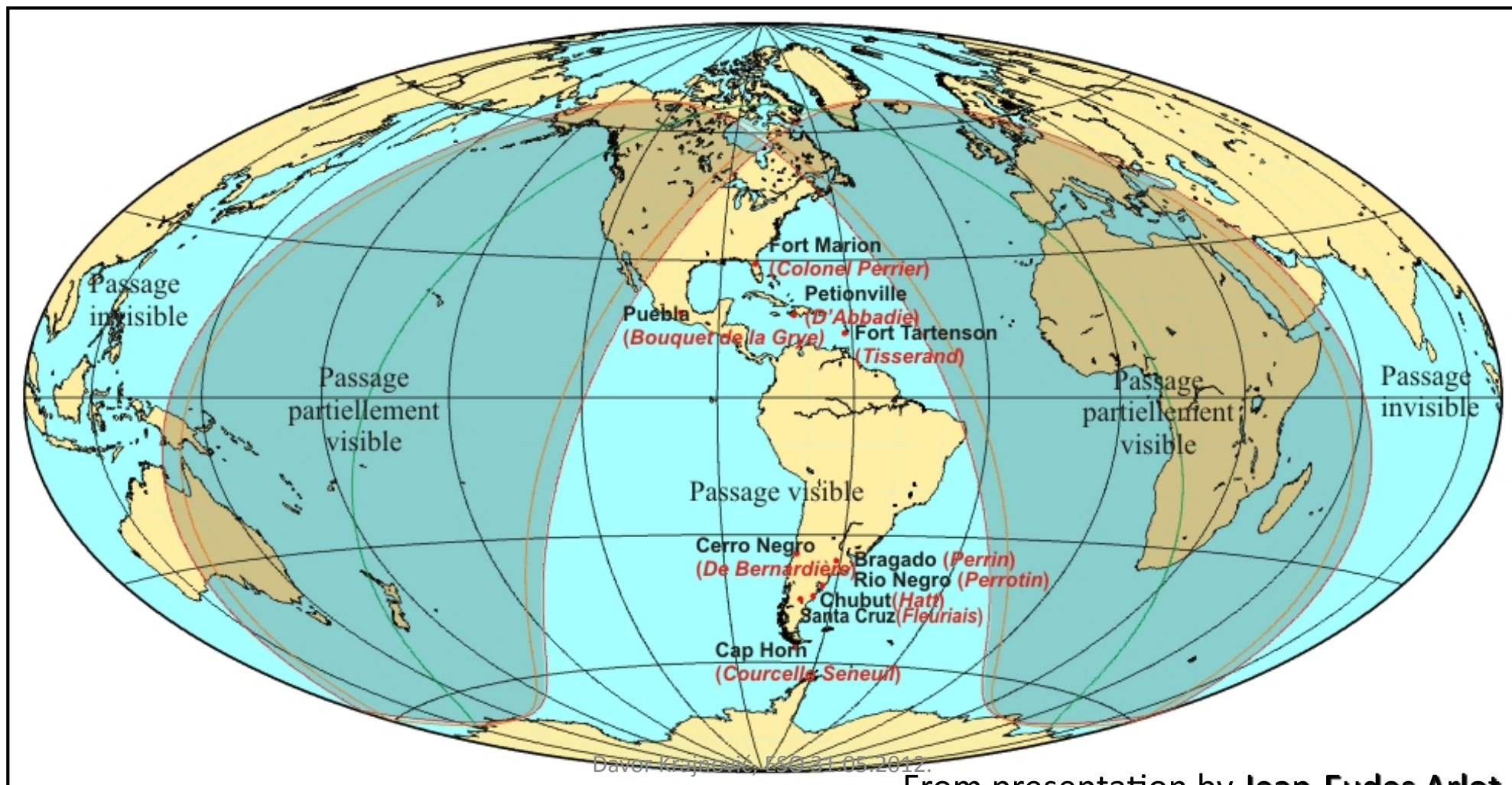


Dupin: Transit of Venus for
Paris Observatory



Members of an
Australian
expedition

Voyages of 1882



From presentation by **Jean-Eudes Arlot**

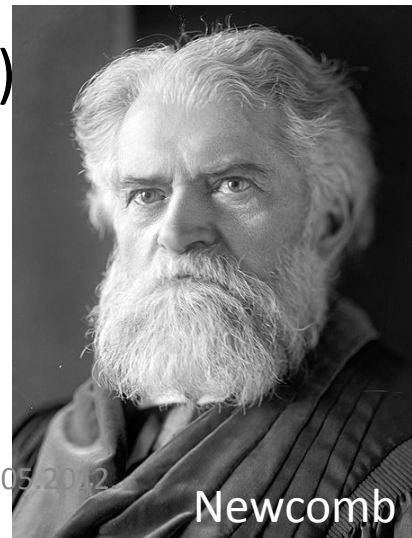
Results of XIX century

- Anticlimax
- Solar Parallax: $8.79'' - 8.88''$
- AU = 147 960 000 – 149 480 000 km
- Simon Newcomb
 - Used data from both 18th and 19th century
 - $8.79'' \pm 0.05''$ (18th century)
 - $8.79'' \pm 0.02''$ (18+19th century)
 - Reached Halley's estimate
- David Gill
 - Solar parallax from Mars
 - $8.78'' \pm 0.01''$

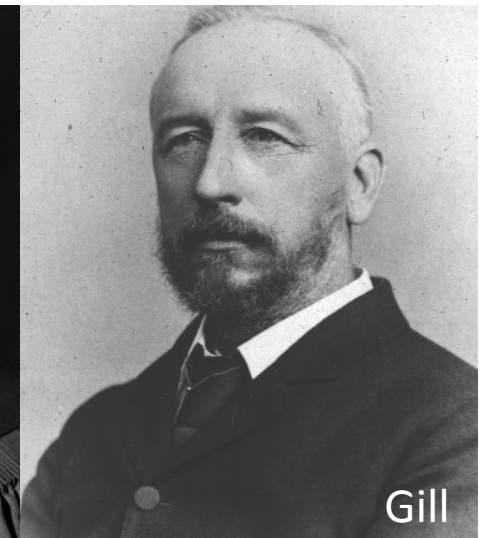
1 AU TODAY:

$8.794148''$

149 597 870 km



Newcomb



Gill

Summary of AU measurements

Epoch	AU [km]	Error [km]	Diff to today AU	who
1 st BC	78 540 000	Unknown	71 057 900	Posidonius*
2 nd – 16 th	7 206 000	Unknown	140 958 000	Ptolomy*
17 th	94 000 000	Unknown	55 597 870	Horrocks
1761	138 540 000	14 400 000	11 057 870	Pingré & Short
1761 & 1769	151 000 000	1 500 000	1 402 130	Lalande&Pingré
1761 & 1769	149 670 000	850 000	72 130	Newcomb
1874 & 1882	149 670 000	330 000	72 130	Newcomb
1931	149 675 000	17 000	77 136	Spencer Jones^
2004	149 608 708	11 835	10 838	VT-2004

- * estimates based on uncertain assumptions
- ^ parallax of Eros

Resources

- Big thanks to our Librarians: Uta and Silvia!
- Eli Maor: *“June 8, 2004: Venus in Transit”*, 2000, Princeton, PUP
- Richard Proctor: *“Transits of Venus”*, 1882, London, Longmans, Green & Co.
- Harry Woolf: *“The Transits of Venus, A study of Eighteenth-century Science”*, 1959, Princeton, PUP
- Harm Habing, *“Kosmos”*, 2009, Diemen, Veen Magazines
- Papers
 - Proceedings of the IAU – Volume 2004, Issue IAUC 196
 - IAU Resolutions 1976
 - Launay & Hingley, 2005, JHA, 36, 57
- Wikipedia
- www.transitofvenus.org (+ F. Espenak)
- www.exploratorium.edu
- www.eso.org/public/outreach/eduoff/vt-2004/
- www.endeavourvoyages.com.au/



The last in our lives

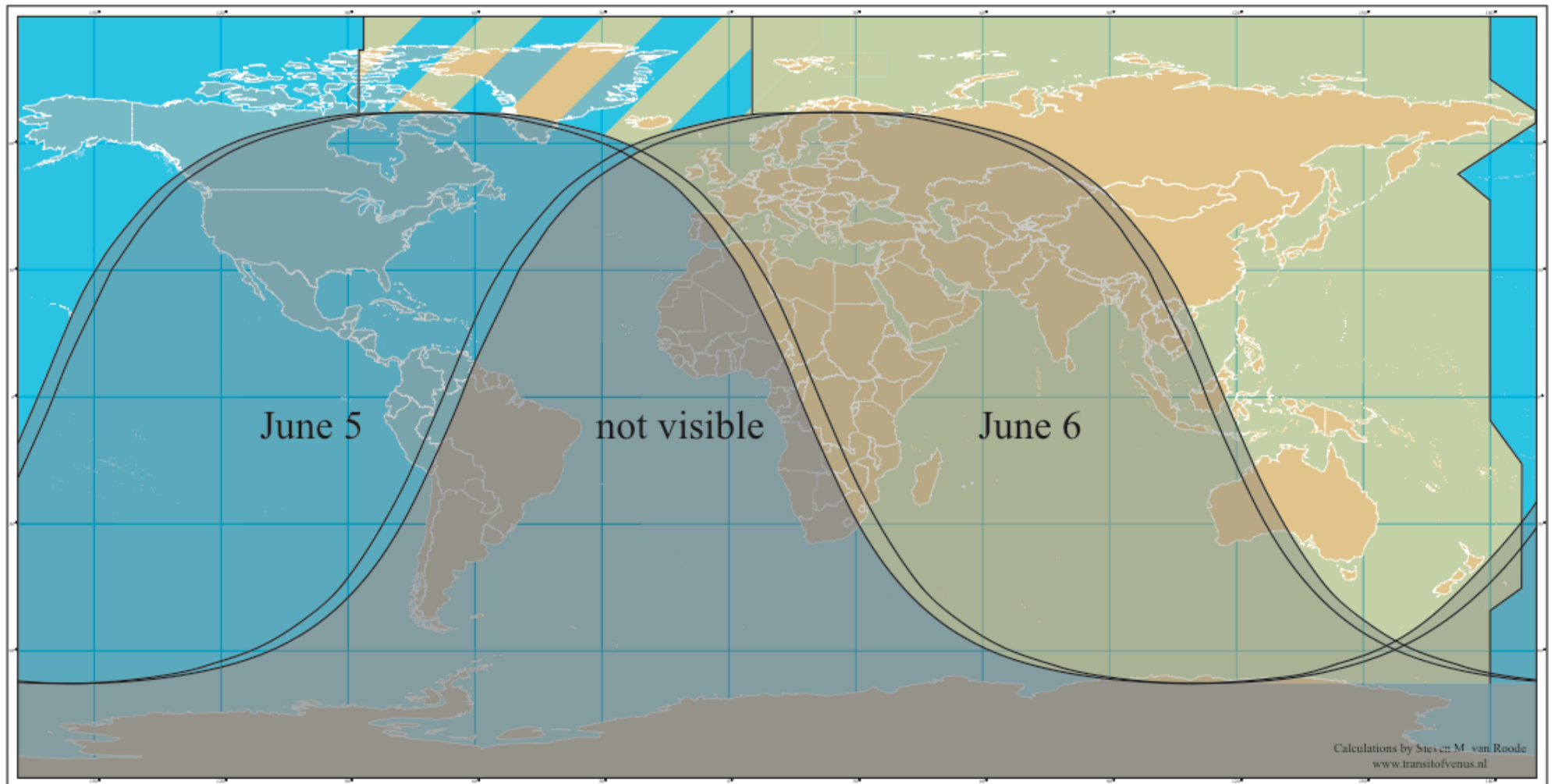


FIGURE 2
Transit of Venus of 2012 June 05/06

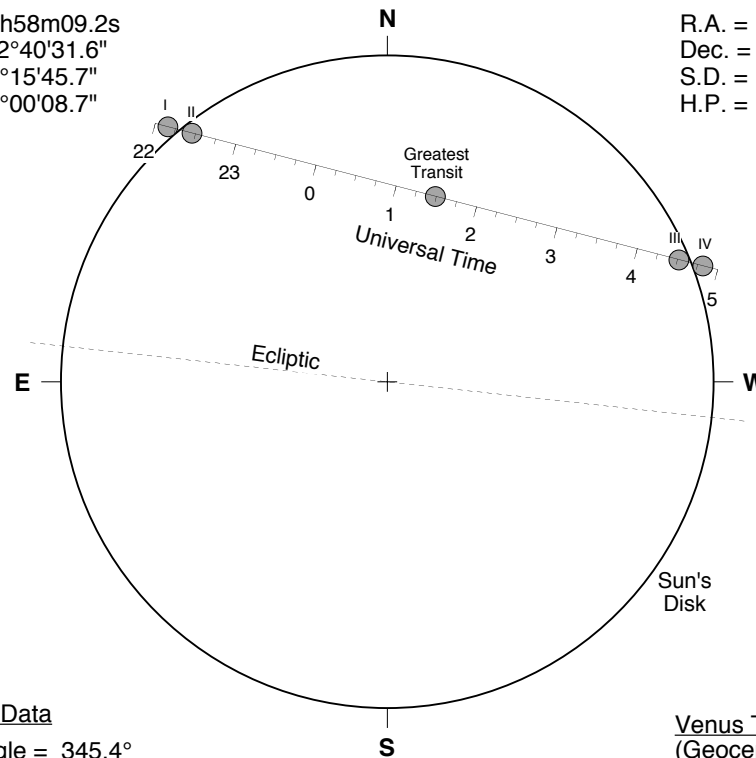
Greatest Transit = 01:29:36.3 UT J.D. = 2456084.562225

Sun at Greatest Transit
 (Geocentric Coordinates)

R.A. = 04h58m09.2s
 Dec. = +22°40'31.6"
 S.D. = 00°15'45.7"
 H.P. = 00°00'08.7"

Venus at Greatest Transit
 (Geocentric Coordinates)

R.A. = 04h57m58.8s
 Dec. = +22°49'25.9"
 S.D. = 00°00'28.9"
 H.P. = 00°00'30.5"

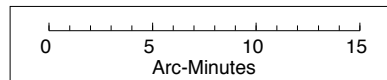


Geocentric Data

Position Angle = 345.4°
 Separation = 554.4"
 Duration = 06h40m

Ephemeris Data

Eph. = VSOP87
 ΔT = 66.7 s



F. Espenak, NASAs GSFC - 2011 Jun
eclipse.gsfc.nasa.gov/OH/transit12.html

Venus Transit Contacts
 (Geocentric Coordinates)

I = 22:09:38 UT
 II = 22:27:34 UT
 Greatest = 01:29:36 UT
 III = 04:31:39 UT
 IV = 04:49:35 UT